

Structured Questions

Radioactive Decay

Isotopes & Radioactive Decay / Background Radiation / Alpha, Beta & Gamma Particles / Radioactive Decay Equations / Activity & Half-Life / Decay Constant & Half-Life (HL) / The Law of Radioactive Decay (HL) / Applications of Radioactivity / Mass Defect & Nuclear Binding Energy / Binding Energy per Nucleon Curve / Nuclear Stability (HL) / Nuclear Energy Levels (HL) / Evidence for the Neutrino (HL)

Easy (8 questions)	/112
Medium (10 questions)	/98
Hard (7 questions)	/58
Total Marks	/268

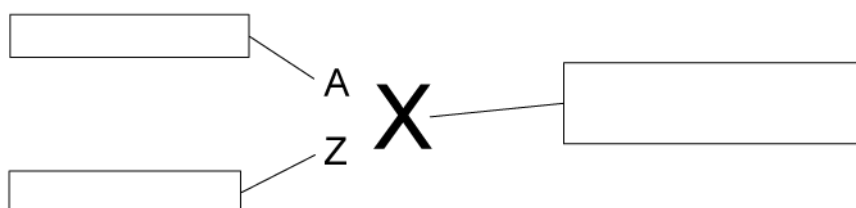
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Easy Questions

1 (a) Nuclides can be written in symbol form.

Complete the labels on the general nuclide symbol using the words below:



- Chemical symbol for the element
- Proton number
- Nucleon number

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(3 marks)

(b) Define radioactive decay.

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(4 marks)

(c) Draw lines to match the phrases with the correct definitions.

A spontaneous process
A random process
Isotopic data

A process in which the exact time of decay of a nucleus cannot be predicted
The relative amounts of different isotopes of an element found within a substance
A process which cannot be influenced by environmental factors

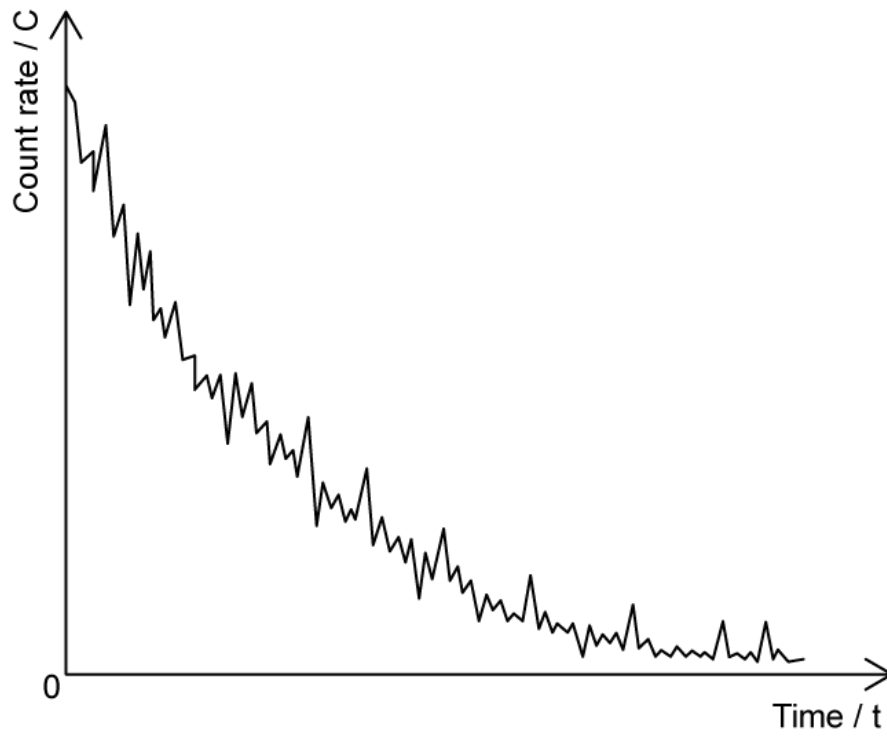
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(3 marks)

- (d) The graph shows the count rate of a radioactive substance measured by a Geiger-Müller tube.



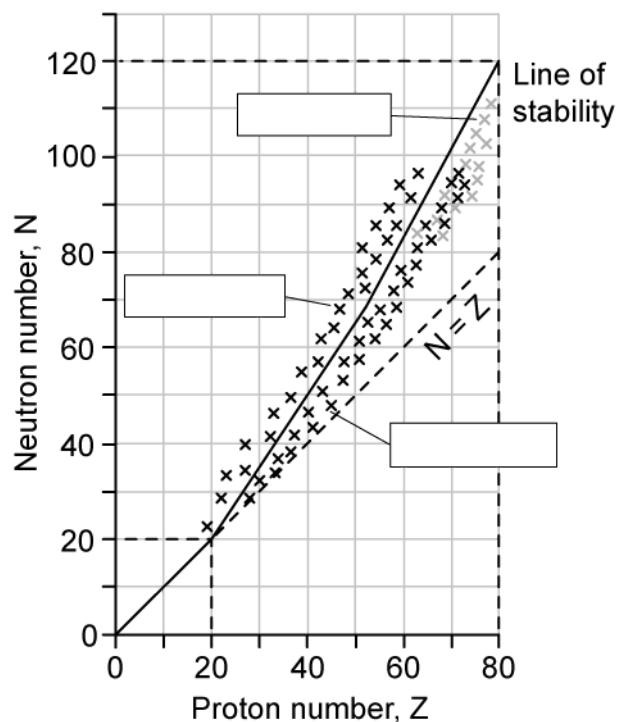
State what the fluctuations in the count rate provide evidence for.

(1 mark)

- 2 (a) The number of neutrons and number of protons for different isotopes can be plotted on a graph called a nuclear stability curve. Different regions on the graph represent the type of decay which is expected.

The three types of radioactive particles shown are alpha emitters, beta-minus emitters and beta-positive emitters.

Label the regions of the graph to indicate which type of radioactive particle is expected to be emitted.



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(3 marks)

- (b) Background radiation comes from a variety of sources, some are natural and some are man-made.

Place ticks (✓) in the correct column to indicate whether the source is man-made or natural:

	Mad-made source	Natural source
Fallout from nuclear weapons		
Cosmic rays		
Nuclear waste		
Nuclear accidents		
Carbon-14 in biological material		
Radon gas		
Medical sources		
Radioactive material in food and drink		

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(8 marks)

(c) Radiation is emitted as various different types of particle.

State 4 types of radioactive particle.

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(4 marks)

(d) When a beta emission occurs, a particle called a neutrino is also emitted.

Complete the gaps in the following sentences. Choose from the words below:

A neutrino has no _____ and negligible _____. Electron anti-neutrinos are produced during _____ decay. Electron neutrinos are produced during _____ decay.

mass gravity age charge beta-minus beta-positive alpha

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(4 marks)

3 (a) Complete the table with the correct properties of alpha, beta-minus, beta-positive and gamma radiation.

Particle	Composition	Mass / u	Charge / e
Alpha	2 protons and 2 neutrons		
Beta-minus		0.0005	-1
Beta-plus	Positron (e ⁺)	0.0005	
Gamma			0

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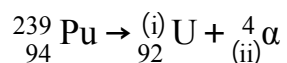
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(6 marks)

(b) Plutonium-239 decays to Uranium-235 through the emission of an alpha particle.

Determine the missing values in the decay equation:



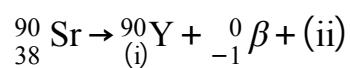
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(2 marks)

(c) Strontium-90 decays through beta-minus decay to form Yttrium-90.

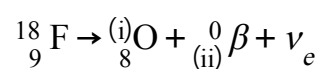
Determine the missing values in the decay equation.



(2 marks)

(d) Fluorine-18 decays through beta-plus decay to form oxygen-18.

Determine the missing values in the decay equation.



(2 marks)

4 (a) Define:

(i) Binding energy.

[1]

(ii) Mass defect.

[1]

(2 marks)

(b) The nuclear rest mass of oxygen-16 ($^{16}_8\text{O}$) is 15.994 914 u.

The mass defect, Δm , equation describes the relationship between the proton number, Z , the number of neutrons, N , the proton rest mass, m_p , the neutron rest mass, m_n , and the nuclear rest mass, m_{total} .

$$\Delta m = Zm_p + Nm_n - m_{\text{total}}$$

Calculate the mass defect of oxygen-16. Give your answer to 6 d.p.

(4 marks)

(c) The mass defect (from part (b)) can be used to calculate the binding energy.

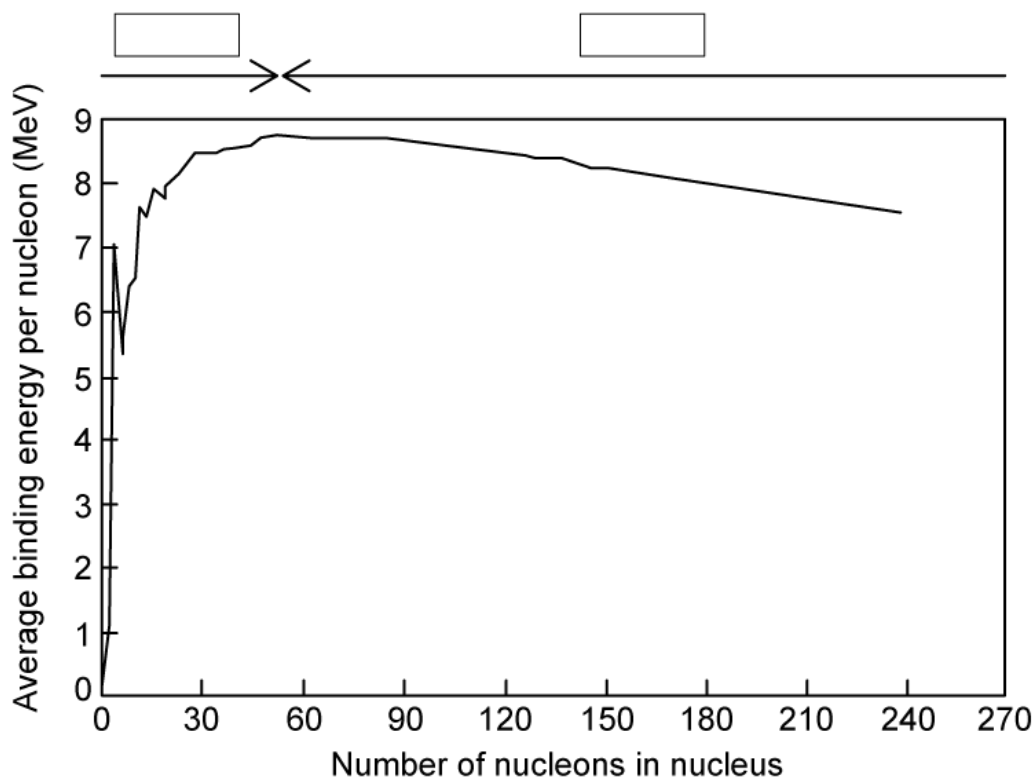
Calculate the total binding energy for a nucleus of oxygen-16 in J

(3 marks)

(d) Determine the binding energy per nucleon of oxygen-16 in J.

(2 marks)

5 (a) The chart shows the binding energy per nucleon for a number of nuclei.



Label the chart to show:

- (i) Where fusion of these elements occurs to release energy [1]
- (ii) Where fission of these elements occurs to release energy [1]
- (iii) The location of Iron (${}_{26}^{56}\text{Fe}$) by drawing an X [1]

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(3 marks)

(b) In terms of the forces acting within the nucleus, explain why:

(i) Fusion occurs for nuclides with low nucleon numbers.

[2]

(ii) Fission occurs for nuclides with high nucleon numbers.

[2]

(4 marks)

(c) In both fission and fusion, there is a mass defect between the original nuclei and the daughter nuclei.

Complete the sentences by circling the correct word.

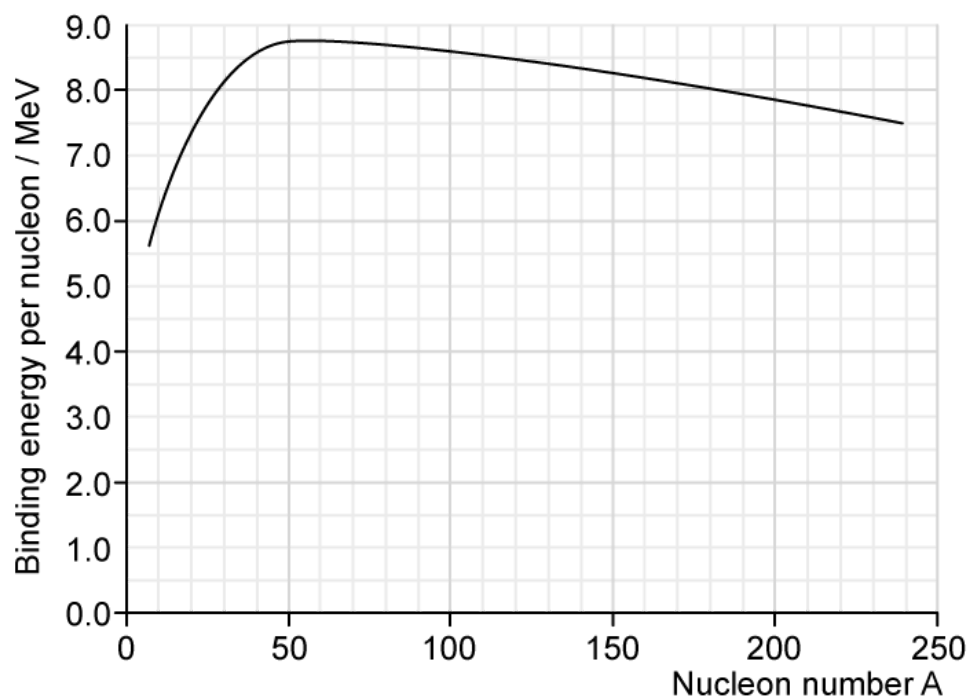
In fusion, the mass of the nucleus that is created is slightly **more / less** than the total mass of the original nuclei and the daughter nucleus is **more / less** stable.

In fission, an unstable nucleus is converted into more stable nuclei with a **larger / smaller** total mass. In both cases, this difference in mass, the mass defect, is equal to the binding energy that is released.

Fission / Fusion releases much more energy per kg than **fission / fusion**. The greater the increase in binding energy, the **more / less** energy is released.

(4 marks)

(d) The graph shows the binding energy per nucleon in MeV plotted against nucleon number, A.

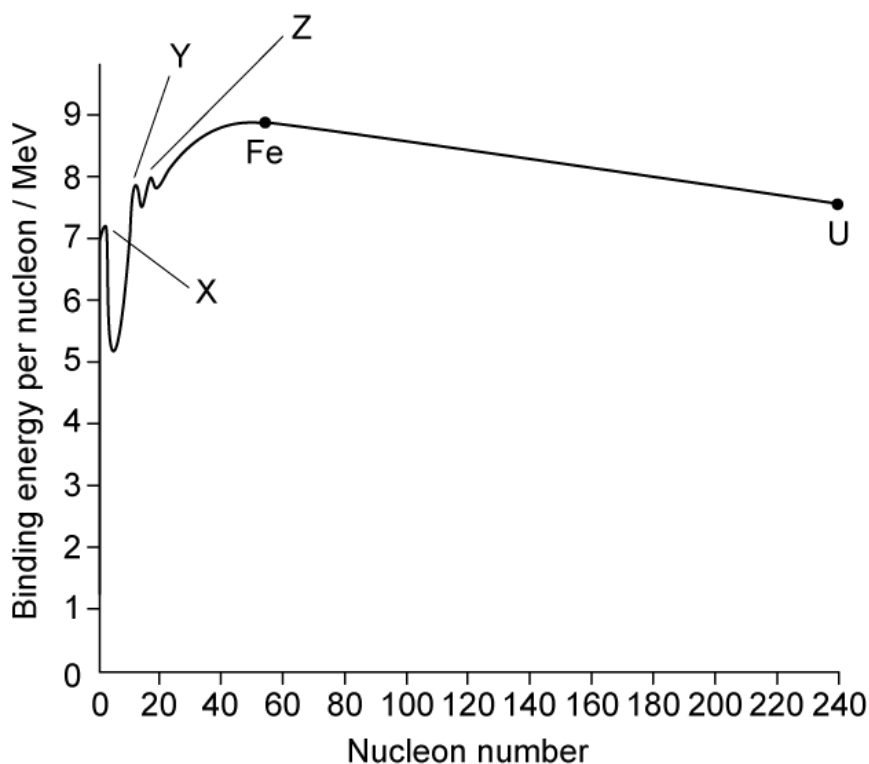


Use the graph to find the binding energy of the following nuclei.

- (i) Platinum-190. [1]
- (ii) Silicon-28. [1]
- (iii) Tellurium-120. [1]

(3 marks)

6 (a) The graph below shows the binding energy per nucleon against the number of nucleons in the nucleus.



There are three nuclei, labelled X, Y and Z, which do not sit on the line of the graph.

Match up the labels to the correct element by drawing a line between the boxes

X

Oxygen

Y

Helium

Z

Carbon

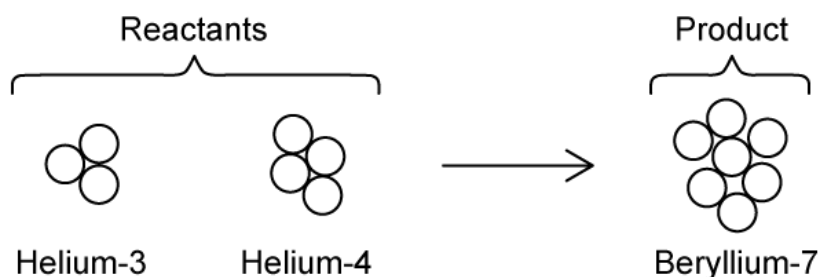
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(3 marks)

(b) Helium can fuse together to form beryllium as shown in the reaction below:



State and explain which is larger, the mass of the reactants or the mass of the products.

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(3 marks)

(c) The table shows the mass of each reactant and daughter nucleus:

Nucleus	Mass / u
Helium - 3	3.01493
Helium - 4	4.00151
Beryllium - 7	7.01473

Using the information in the table:

(i) Calculate the mass of the reactants, m_R in atomic mass units. [2]

(ii) Calculate the mass defect, Δm , between the reactants and the daughter nuclei in atomic mass units. [3]

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(5 marks)

(d) Helium-3 and helium-4 fuse together to form beryllium-7.

The mass defect, Δm for this fusion reaction is equal to 2.8×10^{-30} kg.

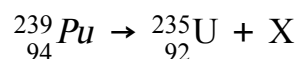
Calculate the energy released, ΔE , in the fusion of beryllium-7.

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(2 marks)

7 (a) Outline what is meant by the term decay constant.

(2 marks)

(b) A sample of 2.5 mol of the radioactive nuclide plutonium-239 decays into uranium-235 with the production of another particle.



- (i) Identify particle X. [1]
- (ii) The radioactive decay constant of plutonium-239 is $9.5 \times 10^{-13} \text{ s}^{-1}$. Determine the time required to produce 1 mol of uranium-235. [4]

(5 marks)

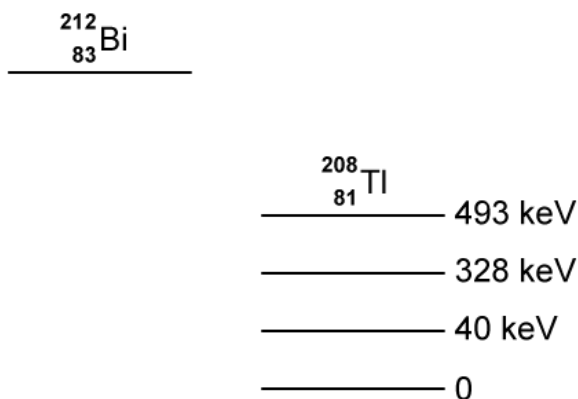
(c) Thorium-227 is one of the isotopes formed after a uranium-235 nucleus has undergone a series of decays.

One sample of thorium-227 has a decay constant of 0.037 day^{-1} and an initial activity of 46 Bq.

- (i) State what is meant by the activity of a sample. [2]
- (ii) Calculate the activity of the sample after one week. [3]

(5 marks)

- 8 (a) The isotope bismuth-212 undergoes α -decay to an isotope of thallium-208. In this decay, a gamma-ray photon is also produced.



- (i) Complete the nuclear energy level diagram to indicate the alpha decay of Bi-212 into Tl-208, followed by the emission of a photon of energy 0.493 MeV. [2]
- (ii) Outline how the alpha particle spectrum and the gamma spectrum of the decay of bismuth-212 give evidence for the existence of discrete nuclear energy levels, by completing the following sentences:

The emitted alpha particles have energies.

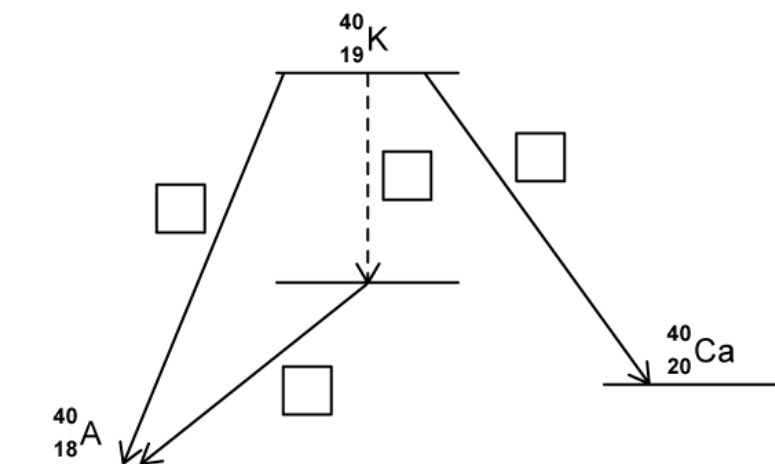
The emitted gamma rays have energies.

Therefore, nuclear energy levels must be discrete because the energies of the alpha particles and the gamma photons are determined by

[3]

(5 marks)

- (b) The isotope potassium-40 can decay via different decay modes to form isotopes of argon-40 or calcium-40.



- (i) Complete the nuclear energy level diagram to indicate the different modes of decay.

[3]

- (ii) Outline how the β spectrum of the decay of potassium-40 led to the existence of the neutrino being postulated, by completing the following sentences:

The total energy released in any beta decay is, however, the majority of beta particles are found to have energies than this value.

The distribution of energy values for the beta particles is not, it is found to be a spectrum.

The existence of the neutrino was postulated to account for the

The total energy of the decay process must be divided between the and

[2]

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(5 marks)

- (c) The isotope potassium-40 occurs naturally in many rock formations. The composition of a particular rock sample is found to be 33% potassium-40 atoms out of the total number of argon and potassium-40 atoms.

The half-life of potassium-40 is 1.3×10^9 years.

Determine the age of the rock sample.

(4 marks)

- (d) Bismuth-212 is a short-lived isotope with a half-life of 1 hour.

Briefly outline experimental methods which can measure the half-life of:

- (i) Bismuth-212 [3]
- (ii) Potassium-40 [3]

(6 marks)

Medium Questions

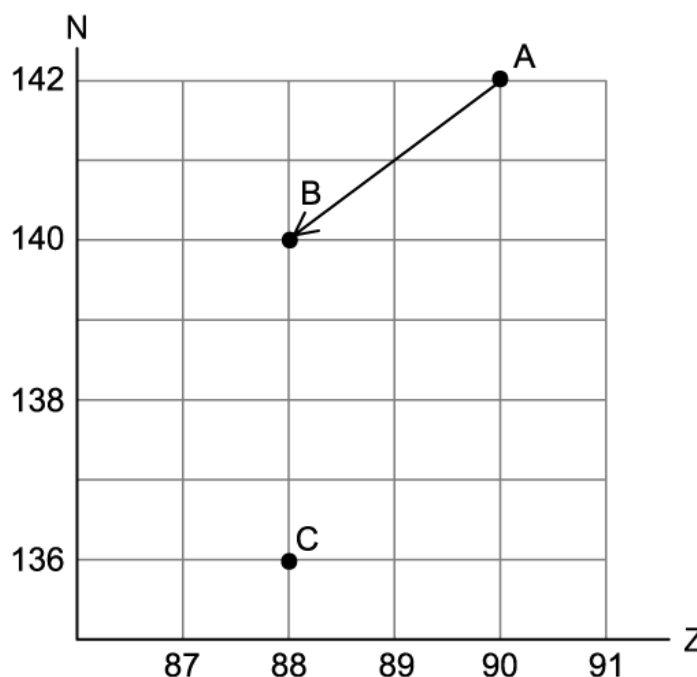
- 1 (a) The decay series of an isotope of thorium ($^{232}_{90}\text{Th}$) produces an isotope of radium ($^{224}_{88}\text{Ra}$). This process involves four separate decays.

The first decay involves the emission of an alpha particle.

Write the decay equation for this process, including the symbol of the daughter product.

(3 marks)

- (b) The first decay can be represented on an N-Z diagram as an arrow from point A to point B.



Three more decays occur before $^{224}_{88}\text{Ra}$ is produced, denoted by "C" on the N-Z diagram.

Outline the possible sequence of decays which lead from point B to C.

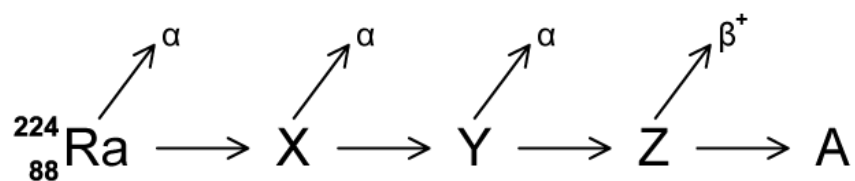
(3 marks)

(c) Nuclei can be unstable for a number of reasons.

In terms of forces within the nucleus, explain why large nuclei emit alpha radiation.

(4 marks)

(d) ${}^{224}_{88}\text{Ra}$ then decays four more times, shown below.



The first three decays result in the emission of an alpha particle each time. The fourth and final decay results in the emission of a beta-particle.

Calculate the nucleon number and atomic number of nuclide A.

(3 marks)

2 (a) A radioactive source is used to measure the thickness of paper. A Geiger counter is used to measure the count rate on the opposite side of the paper to the radioactive source. The radioactive source used must be chosen carefully.

(i) State and explain the type of radioactive source that should be used for this process.

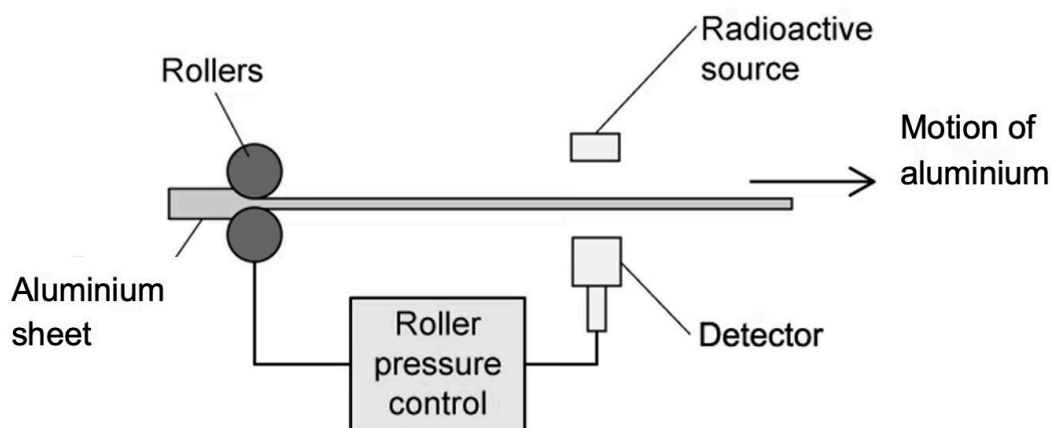
[2]

(ii) A new type of paper is placed between the Geiger counter and the radioactive source. Explain how the equipment can be used to show if the new paper is thicker or thinner than the previous type.

[2]

(4 marks)

(b) The arrangement below is used to maintain a constant 0.10 m thickness of aluminium sheets. Alpha, beta or gamma sources are available to be used.



Outline the most suitable radioactive source for this arrangement and explain why the other sources may not be appropriate.

(2 marks)

- (c)** The source used in part (b) has a half-life of 14 days and it has an initial count rate of 240 counts per minute when first used in the apparatus.

Giving your answer in weeks, calculate the length of time it takes for the Geiger counter to detect a count rate of 0.25 s^{-1} .

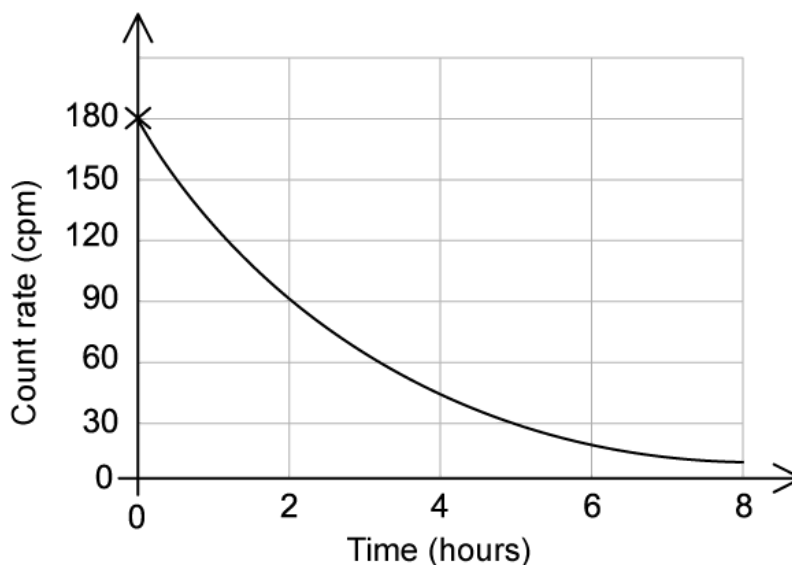
(3 marks)

- (d)** Once the source has reached an activity of 0.25 s^{-1} , it is replaced as the count rate of the source is comparable with that of background radiation.

State two natural sources of background radiation and two man-made sources of background radiation.

(4 marks)

3 (a) A sample's count rate in counts per minute (cpm) is measured using a ray detector. This data is plotted on a graph.



(i) Use the graph to determine the half-life of this sample.

[2]

(ii) Explain why the distance between the detector and the source is a control variable.

[2]

(1 mark)

(b) The scientist wonders how the experiment in part (a) would have changed if the sample was twice the size.

Assuming the experiment from part (a) was repeated with a sample the exact same age but twice the mass, calculate the length of time it would have taken to reach a count rate of 22.5 cpm.

(3 marks)

(c) In reality the detector will measure a count rate of more than 5 cpm long after the length of time in part (b) has passed.

(i) Outline the reason for this larger-than-expected count rate.

[2]

(ii) Describe the measurements the scientist could take to accurately account for this additional count rate in the final data.

[2]

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(4 marks)

(d) The scientist can measure the count rate of the source but is unable to directly measure the activity of the source using their detector. Activity is the total number of particles emitted from the sample per unit time.

Explain why this is not possible.

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(2 marks)

- 4 (a) An unstable isotope of mercury, Hg-203, is tested for its radioactive emissions in a laboratory that has a background rate of 0.3 s^{-1} .

A source is placed a fixed distance from a Geiger-Muller tube. Various materials are placed in between the detector and the source while the count rate is recorded. The results are shown below.

Material	Count rate / s^{-1}
None	68
0.5 mm thick paper	69
2.0 mm thick paper	65
5 cm thick aluminium foil	15

State and explain what types of radiation are being emitted by the Hg-203 source.

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(4 marks)

- (b) A student notices that the count rate recorded actually increases when 0.5 mm thick paper was placed between the Geiger-Muller tube and the source.

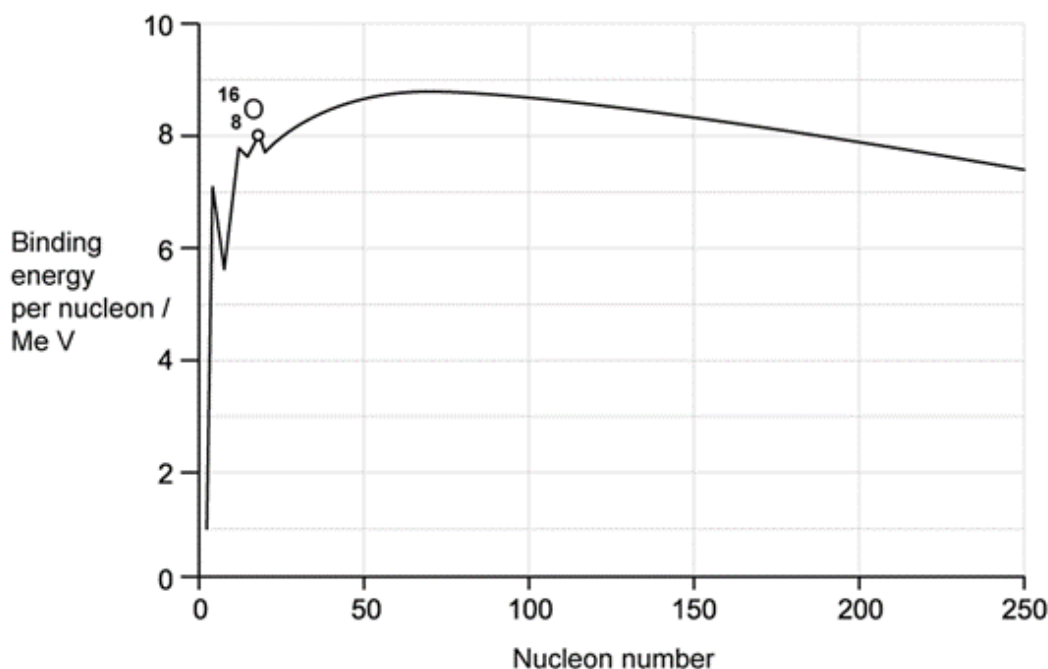
(i) Suggest one cause of this increase. [1]

(ii) Describe what the experimenter could do to check if this data point was anomalous. [2]

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(3 marks)

5 (a) The diagram below shows a plot of binding energy per nucleon against with nucleon number.



Fission and fusion are two nuclear processes in which energy can be released.

(i) On the diagram, mark the element with the highest binding energy per nucleon.

[1]

(ii) Explain why nuclei that undergo fission are restricted to a different part of the graph than those that undergo fusion.

[2]

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(3 marks)

(b) Explain with reference to the figure in part (a), why the energy released per nucleon from fusion is greater than that from fission.

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(3 marks)

- (c) Explain how the binding energy of an oxygen ${}^{16}_8\text{O}$ nucleus can be calculated with information obtained in the figure from part (a).

(2 marks)

- (d) The mass of an ${}^{16}_8\text{O}$ nucleus is 15.991 u.

Calculate:

- (i) The mass difference, in kg, of the ${}^{16}_8\text{O}$ nucleus.

[2]

- (ii) The binding energy, in MeV, of an oxygen ${}^{16}_8\text{O}$ nucleus.

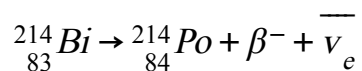
[1]

(3 marks)

6 (a) Bismuth-214 (${}^{214}_{83}\text{Bi}$) decays into Polonium-214 (${}^{214}_{84}\text{Po}$) by beta minus decay.

The binding energy per nucleon of Bismuth-214 is 7.774 MeV and the binding energy per nucleon of Polonium-214 is 7.785 MeV.

Beta-minus decay is described by the following equation:



Show that the energy released in the β^{-} decay of bismuth is about 2.35 MeV and state where the energy comes from.

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(3 marks)

(b) If an additional neutron is accelerated into the Polonium-214 (${}^{214}_{84}\text{Po}$) to produce the isotope Polonium-215 (${}^{215}_{84}\text{Po}$), use the following information to deduce the binding energy per nucleon of this new isotope.

$$\text{Mass of } {}^{215}_{84}\text{Po} \text{ nucleus} = 3.571140 \times 10^{-25} \text{ kg}$$

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(5 marks)

(c) Polonium-215 (${}^{215}_{84}\text{Po}$) is radioactive and decays by the producing alpha radiation, which is known to be a particularly stable.

Determine the binding energy of alpha radiation.

The following information is available:

- Mass of a Helium-4 nucleus: 4.001265 u

(3 marks)

- (d)** A student claims that the amount of matter within a marble directly converted into energy would be enough to provide 1 year of current human energy consumption globally which is estimated to be 5.80×10^{18} J.

If the matter within marble is approximately 6.02×10^{23} u, determine if this statement is true, using the mass-energy equivalence.

(2 marks)

7 (a) Explain why the mass of an alpha-particle (α) is less than the total mass of two individual protons and two individual neutrons.

(2 marks)

(b) Show that the energy equivalence of 1.0 u is 931.5 MeV.

(2 marks)

(c) Data for the masses of some nuclei are given below

Nuclei	Mass / u
Deuterium (2_1H)	2.0141
Zirconium (${}^{97}_{40}Zr$)	97.0980

Use the data to determine the binding energy of deuterium in MeV.

(2 marks)

(d) Using the data given in part (c), determine the binding energy per nucleon of zirconium in MeV.

(3 marks)

8 (a) Iodine-131 ($^{131}_{53}\text{I}$) has a half-life of 8.02 days.

Calculate the decay constant of $^{131}_{53}\text{I}$.

(2 marks)

(b) The initial activity of the sample of iodine-131 is 6.5×10^4 Bq.

Determine the activity after 16 days.

(2 marks)

(c) Determine the mass of the iodine-131 in the sample after 16 days.

(2 marks)

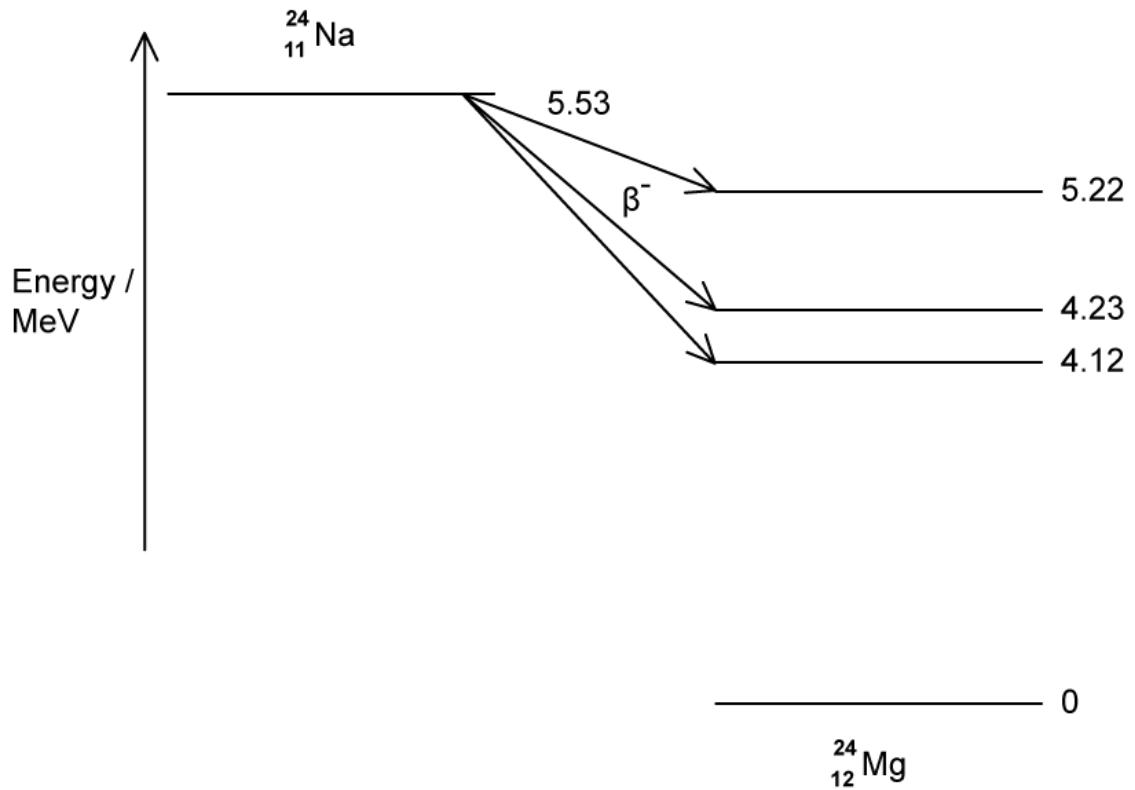
(d) Iodine-131 decays through a number of decay modes. Two of these are β^- decay of 606 keV and gamma emission of 364 keV. The product of the β^- decay is $^{131}_{54}\text{Xe}$.

Sketch a nuclear energy level diagram to represent these decays.

(2 marks)

- 9 (a) A nucleus of sodium-24 decays into a stable nucleus of magnesium-24. It decays by β^- emission followed by the emission of γ -radiation as the magnesium-24 nucleus de-excites into its ground state.

The sodium-24 nucleus can decay to one of three excited states of the magnesium-24 nucleus. This is shown in the diagram below:



The energies of the excited states are shown relative to the ground state.

Calculate the maximum possible speed of the emitted beta particle in MeV.

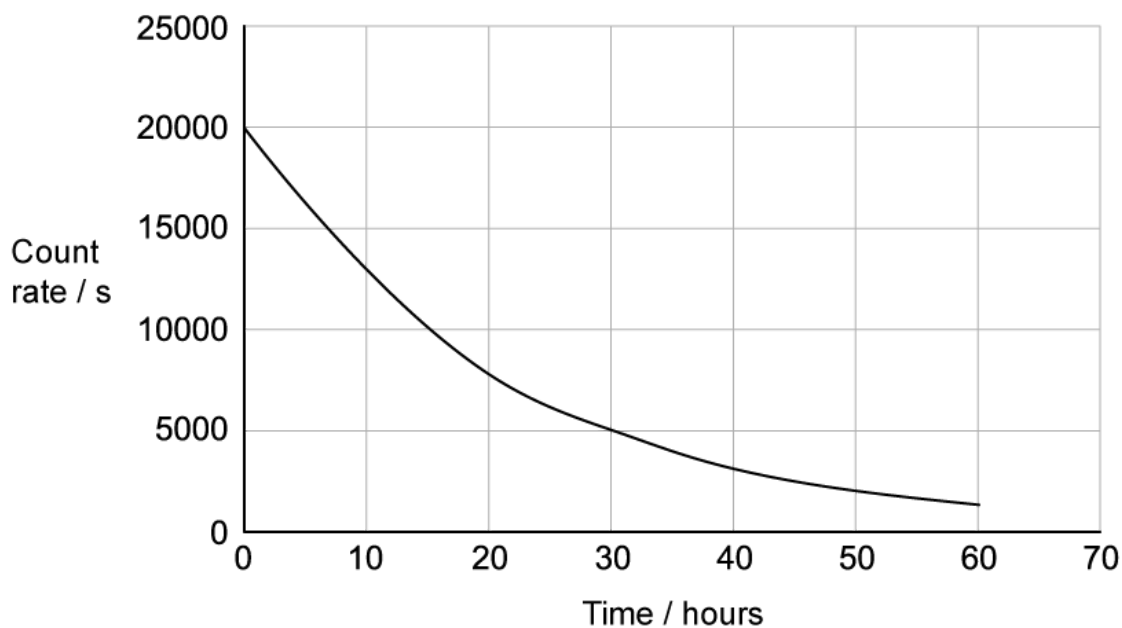
(2 marks)

- (b) The excited magnesium nucleus de-excites through production of gamma radiation of discrete wavelengths.

Calculate the shortest wavelength of emitted radiation.

(3 marks)

(c) The graph shows the activity of a sample of sodium-24 with time.



Use the graph to calculate the decay constant of sodium-24.

(2 marks)

(d) The detector in this experiment measures 4% of the activity from the sample.

Determine the activity of sample after 27 hours from the start of the recording,

(3 marks)

10 (a) Americium-241 has a half-life of 432 years. A small sample is held in a school for use in experiments.

The teacher uses a Geiger-Müller counter to measure the count rate at close range. The relationship between activity and count rate is a ratio of 6:1. Over 5 minutes, the count is 13 600.

Determine the activity of the sample.

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(2 marks)

(b) Determine the activity of the americium sample after 748 years.

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(2 marks)

Hard Questions

- 1 (a) A radioactive nucleus ${}_{85}^{229}\text{X}$ undergoes a beta-minus decay followed by an alpha decay to form a daughter nucleus ${}_{Z}^{\text{A}}\text{Y}$.

Write a decay equation for this interaction and hence determine the values of A and Z.

(2 marks)

- (b) Thorium (${}_{90}^{232}\text{Th}$) decays to an isotope of Radium (Ra) through a series of transformations.

The particles emitted in successive transformations are:

$$\alpha \beta^{-} \beta^{-} \gamma \alpha$$

Determine the resulting nuclide after these successive transformations.

Clearly show how you arrive at your final answer.

(3 marks)

- (c) Through a combination of successive alpha and beta decays, the isotope of any original nucleus can be formed.

Determine the simplest sequence of alpha and beta decays required to do this and explain your reasoning.

(3 marks)

- (d)** A nucleus of bohrium (${}^X_{\text{Y}}\text{Bh}$) decays to mendelevium (${}^{255}_{101}\text{Md}$) by a sequence of three alpha particle emissions.

Determine the number of neutrons in a nucleus of bohrium.

(2 marks)

2 (a) The table shows some of the isotopes of phosphorus and, where they are unstable, the type of decay.

Isotope	$^{29}_{15}\text{P}$	$^{30}_{15}\text{P}$	$^{31}_{15}\text{P}$	$^{32}_{15}\text{P}$	$^{33}_{15}\text{P}$
Type of decay	β^+	β^+	stable		β^-

State whether the isotope $^{32}_{15}\text{P}$ is stable or not. If not, determine, with a reason, the type of decay it experiences.

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(3 marks)

(b) The isotope of phosphorus ($^{30}_{15}\text{P}$) decays into an isotope of silicon (^A_ZSi).

(i) Determine the values of A and Z and write a decay equation for this process.

[2]

(ii) Explain why each emission product occurs.

[2]

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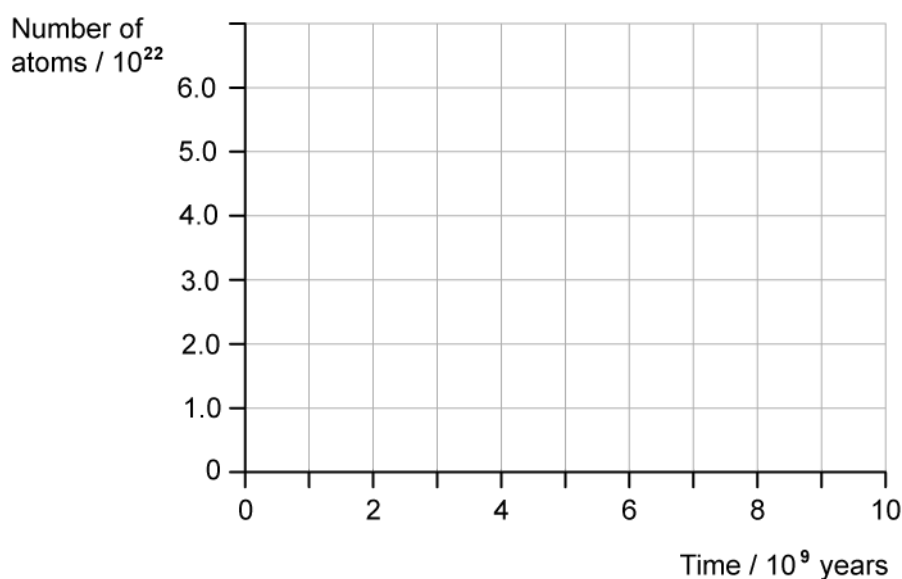
(4 marks)

3 (a) The radioactive isotope uranium-238 decays in a decay series to the stable lead-206.

The half-life of ${}_{92}^{238}\text{U}$ is 4.5×10^9 years, which is much larger than all the other half-lives of the decays in the series.

A rock sample, when formed originally, contained 6.0×10^{22} atoms of ${}_{92}^{238}\text{U}$ and no ${}_{82}^{206}\text{Pb}$ atoms. At any given time, most of the atoms are either ${}_{92}^{238}\text{U}$ or ${}_{82}^{206}\text{Pb}$ with a negligible number of atoms in other forms in the decay series.

Sketch on the axes below the variation of number of ${}_{92}^{238}\text{U}$ atoms and the number of ${}_{82}^{206}\text{Pb}$ atoms in the rock sample as they vary over a period of 1.0×10^{10} years from its formation. Label your graphs U and Pb.



(2 marks)

(b) A certain time, t , after its formation, the sample contained twice as many ${}_{92}^{238}\text{U}$ atoms as ${}_{82}^{206}\text{Pb}$ atoms.

Show that the number of ${}_{92}^{238}\text{U}$ atoms in the rock sample at time t was 4.0×10^{22} .

(2 marks)

- (c) The ratio of the number of lead nuclei N_{Pb} to the number of uranium nuclei N_U at some time t is given by:

$$\frac{N_{Pb}}{N_U} = e^{\lambda t} - 1$$

λ is the decay constant and has a value of 1.54×10^{-10} years.

Calculate the time taken (in years) for there to be twice as many ${}_{92}^{238}\text{U}$ atoms as ${}_{82}^{206}\text{Pb}$ atoms.

(2 marks)

- (d) Lead-214 is an unstable isotope of lead-206. It decays by emitting a β^- particle to form bismuth-214 (Bi)

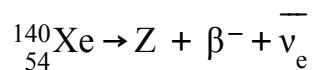
Bismuth is also unstable and has two decay modes:

- Emitting an α particle to form thallium-210 (Tl) + energy
- Emitting a β particle to form polonium-214 (Po) + energy

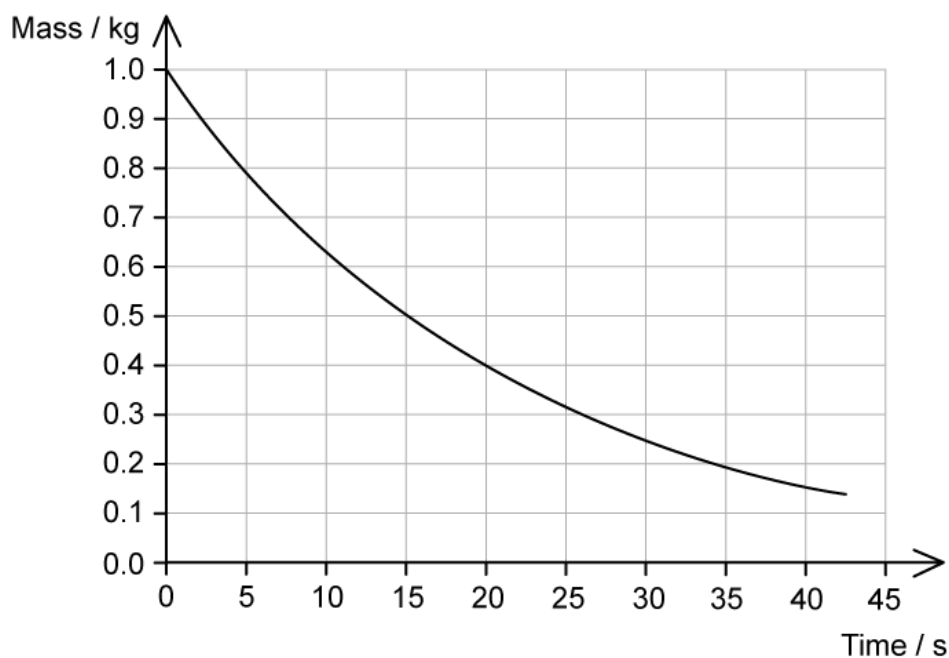
Write decay equations for the decay chain of lead-214 to thallium-210 and to polonium-214. Comment on the nature of the energy released.

(4 marks)

- 4 (a) Xenon-140 ${}^{140}_{54}\text{Xe}$ is one of the waste products from the fission of uranium-235. Xenon-140 is radioactive and decays through β^- decay.



The graph shows the variation with time of the mass of 1 kg of xenon-140 remaining in the sample.



- (i) Calculate the proton and mass numbers of nuclide Z. [1]
- (ii) Calculate the mass of xenon-140 remaining in the sample after 2.5 minutes [3]

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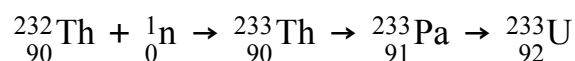
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(4 marks)

- (b) An alternative nuclear fuel to the traditionally used uranium-235 is thorium-232. When thorium-232 is exposed to neutrons, it will undergo a series of nuclear reactions until it eventually emerges as an isotope of uranium-233, which will readily split and release energy the next time it absorbs a neutron.

Part of the thorium fuel cycle is shown below.



Once the uranium-233 nucleus absorbs a neutron, it undergoes fission, releasing energy and two neutrons and forming the fission products Xenon and Strontium as in parts a-c. Any isotopes of uranium-233 which do not undergo fission decay through a chain ending with a stable nucleus of thallium-205 (${}_{81}^{205}\text{Tl}$).

Show that 12 particles, not including neutrons, are emitted during this combination of decay chains. Explain your reasoning.

(4 marks)

5 (a) Show that the decay constant is related to the half-life by the expression

$$\lambda T_{1/2} = \ln 2$$

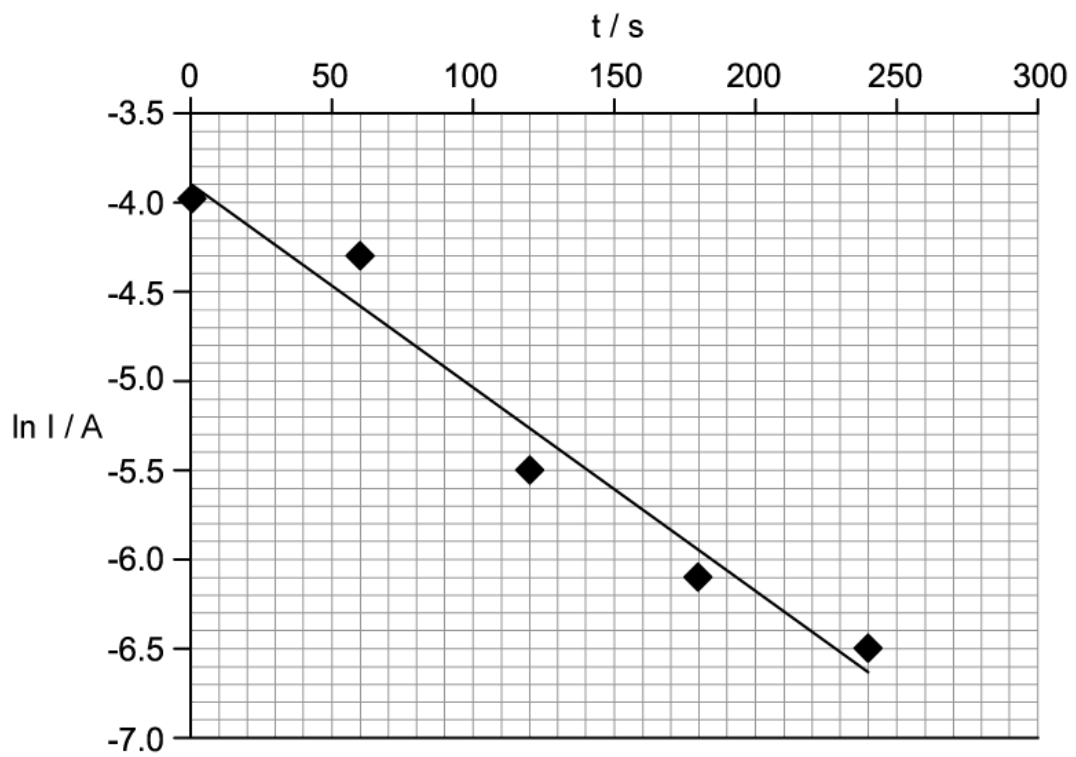
(3 marks)

(b) Uranium-238 has a half-life of 4.47×10^9 years and decays to thorium-234. The thorium decays (by a series of further nuclear processes with short half-lives) to lead.

Assuming that a rock was originally entirely uranium and that at present, 1.5% of the nuclei are now lead, calculate the age of the rock. Give your answer in years to 2 significant figures.

(3 marks)

(c) The ionisation current I produced by α -particles emitted in the decay of radon can be measured experimentally. The logarithmic graph shows how current, $\ln I$, varies with time, t .



Using the graph, determine the half-life of radon.

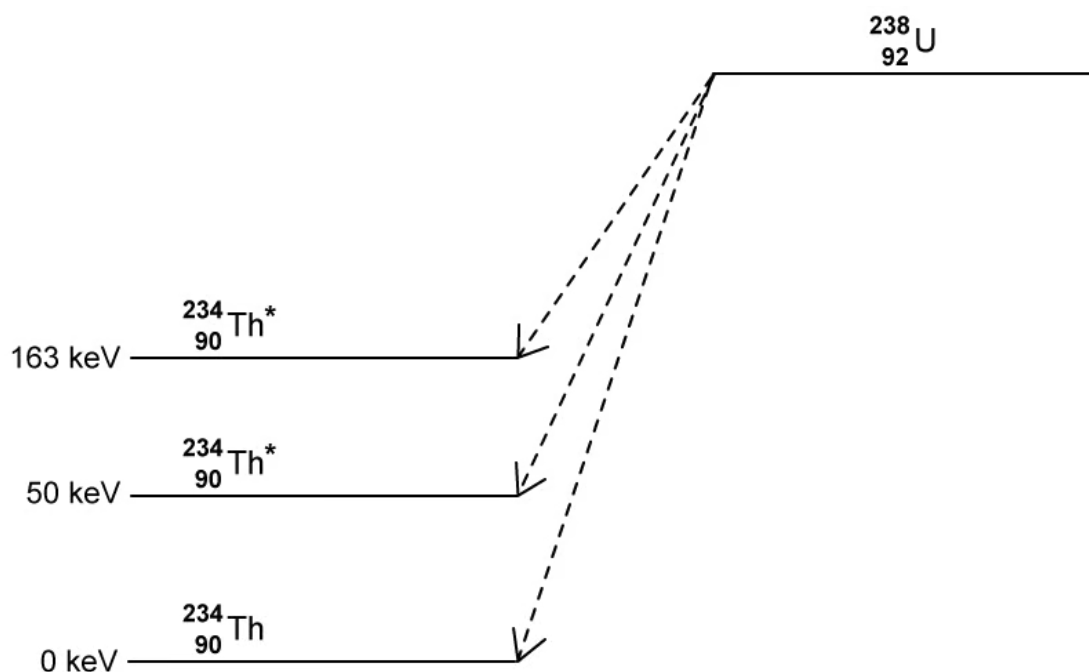
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(3 marks)

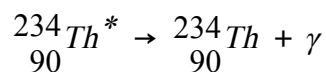
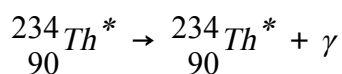
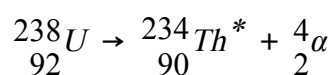
- 6 (a) Unstable uranium-238 has various nuclear decay modes to become stable thorium-234. The total amount of energy released when it decays is measured to be 210 keV.



Outline, without calculation, the intermediate decay modes between the unstable uranium-238 to the stable thorium-234.

(2 marks)

- (b) A possible decay chain for uranium-238 is:



Calculate the total amount of energy, in joules, carried away as gamma radiation in this decay chain.

(4 marks)

(c) Deduce an alternative decay chain from unstable uranium-238 to stable thorium-234 which releases the same amount of energy in the form of gamma radiation as in part (b).

Justify your answer with a calculation.

(2 marks)

- 7 (a) The half-life of uranium-238 is so long in comparison to any of the isotopes in its decay chain that we can assume the number of lead-206 nuclei, N_{Pb} at any time is equal to the number of uranium-238 that have decayed.

The number of uranium-238 nuclei N_U at time t is given by the equation:

$$N_U = N_0 e^{-\lambda t}$$

Where N_0 is the number of uranium-238 nuclei at $t = 0$.

Show that the ratio of N_{Pb} to N_U is given by:

$$\frac{N_{Pb}}{N_U} = e^{\lambda t} - 1$$

(3 marks)

- (b) Enriched uranium fuel is a mixture of the fissionable uranium-235 with the more naturally abundant uranium-238. Mixtures of radioactive nuclides such as this are very common in the nuclear power industry.

Two samples of radioactive nuclides X and Y each have an activity of A_0 at $t = 0$. They are subsequently mixed together.

The half-lives of X and Y are 16 and 8 years respectively.

Show that the total activity of the mixture at time $t = 48$ years is equal to:

$$\frac{9}{64} A_0$$

(3 marks)