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DP IB Maths: AA SL



2.1 Linear Functions & Graphs

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2.1.1 Equations of a Straight Line

Your notes

Equations of a Straight Line

How do I find the gradient of a straight line?

- Find two points that the line passes through with coordinates (x_1, y_1) and (x_2, y_2)
- The gradient between these two points is calculated by

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

- This is given in the formula booklet
- The gradient of a straight line measures its **slope**
 - A line with gradient 1 will go up 1 unit for every unit it goes to the right
 - A line with gradient -2 will go down two units for every unit it goes to the right

What are the equations of a straight line?

- y = mx + c
 - This is the gradient-intercept form
 - It clearly shows the gradient m and the y-intercept (0, c)

$$y - y_1 = m(x - x_1)$$

- This is the point-gradient form
- It clearly shows the gradient m and a point on the line (x_1, y_1)
- ax + by + d = 0
 - This is the **general form**
 - You can quickly get the x-intercept $\left(-\frac{d}{a},0\right)$ and y-intercept $\left(0,-\frac{d}{b}\right)$

How do I find an equation of a straight line?

- You will need the gradient
 - If you are given two points then first find the gradient
- It is easiest to start with the point-gradient form
 - then rearrange into whatever form is required
 - multiplying both sides by any denominators will get rid of fractions
- You can check your answer by using your GDC
 - Graph your answer and check it goes through the point(s)
 - If you have two points then you can enter these in the **statistics mode** and find the regression line

$$y = ax + b$$



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Examiner Tip

- A sketch of the graph of the straight line(s) can be helpful, even if not demanded by the question
 - Use your GDC to plot them
- Ensure you state equations of straight lines in the format required
 - Usually y = mx + c or ax + by + d = 0
 - Check whether coefficients need to be integers (they usually are for ax + by + d = 0)



Worked example

The line I passes through the points (-2, 5) and (6, -7).

Find the equation of l, giving your answer in the form ax + by + d = 0 where a, b and d are integers to be found.

Your notes

Find the gradient between (-2,5) and (6,-7)

Formula booklet

$$m = \frac{-7 - 5}{6 - 2} = -\frac{3}{2}$$
 Gradient formula $m = \frac{y_2 - y_1}{x_2 - x_1}$

Use the point-gradient formula

Formula booklet Equations of a straight
$$y-y_1 = m(x-x_1)$$

$$(x_i, y_i) = (-2, 5)$$
 $m = -\frac{3}{2}$

$$y - 5 = -\frac{3}{2}(x - \frac{1}{2})$$
 Simplify

$$y-5=-\frac{3}{2}(x+2)$$

$$2(y-5)=-3(x+2)$$
Multiply by denominator
$$2y-10=-3x-6$$
Expand
$$3x+2y-4=0$$
Rearrange

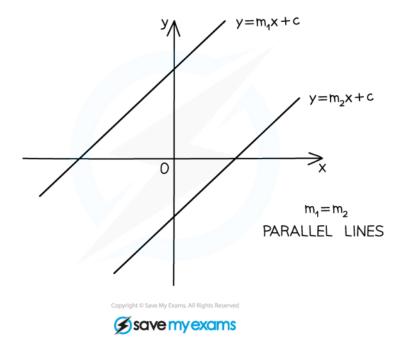


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Parallel Lines

How are the equations of parallel lines connected?

- Parallel lines are always equidistant meaning they never intersect
- Parallel lines have the same gradient
 - If the gradient of line l_1 is m_1 and gradient of line l_2 is m_2 then...
 - $m_1 = m_2 \Rightarrow l_1 \& l_2$ are parallel
 - $I_1 & I_2$ are parallel $\Rightarrow m_1 = m_2$
- To determine if two lines are parallel:
 - Rearrange into the gradient-intercept form y = mx + c
 - lacktriangle Compare the coefficients of X
 - If they are equal then the lines are parallel





Worked example

The line I passes through the point (4, -1) and is parallel to the line with equation 2x - 5y = 3.

Find the equation of l, giving your answer in the form y = mx + c.

Rearrange into
$$y=m\infty+c$$
 to find the gradient $5y=2x-3 \Rightarrow y=\frac{2}{5}x-\frac{3}{5}$: gradient = $\frac{2}{5}$
Parallel lines $\Rightarrow m_1=m_2$
 $m=\frac{2}{5}$

Formula booklet Equations of a straight $y-y_1 = m(x-x_1)$

$$y - y_1 = m(x - x_1)$$

$$(x_1, y_1) = (4, -1)$$
 $m = \frac{2}{5}$

$$y + 1 = \frac{2}{5}(x - 4)$$

$$y + 1 = \frac{2}{5}x - \frac{8}{5}$$

$$y = \frac{2}{5}x - \frac{13}{5}$$

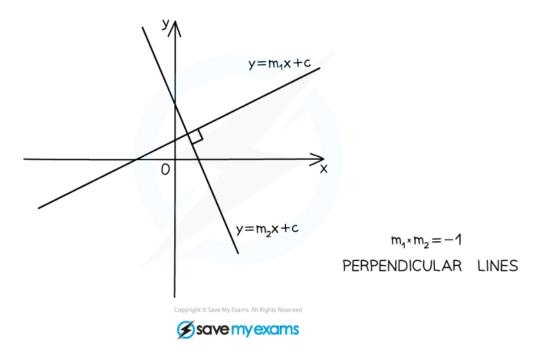




Perpendicular Lines

How are the equations of perpendicular lines connected?

- Perpendicular lines intersect at right angles
- The gradients of two perpendicular lines are negative reciprocals
 - If the gradient of line l_1 is m_1 and gradient of line l_2 is m_2 then...
 - $m_1 \times m_2 = -1 \Rightarrow l_1 \& l_2$ are perpendicular
 - $l_1 \& l_2$ are perpendicular $\Rightarrow m_1 \times m_2 = -1$
- To determine if two lines are perpendicular:
 - Rearrange into the gradient-intercept form y = mx + c
 - lacktriangle Compare the coefficients of X
 - If their product is -1 then they are perpendicular
- Be careful with horizontal and vertical lines
 - x = p and y = q are perpendicular where p and q are constants





Worked example

The line I_1 is given by the equation 3x - 5y = 7.

The line I_2 is given by the equation $y = \frac{1}{4} - \frac{5}{3}x$.

Determine whether $\,I_{1}^{}$ and $\,I_{2}^{}$ are perpendicular. Give a reason for your answer.

$$5y = 3x - 7$$
 => $y = \frac{3}{5}x - \frac{7}{5}$

Identity gradients

$$m_1 = \frac{3}{5}$$
 $m_2 = -\frac{5}{3}$

m, x m2 =-1 => Perpendicular lines

$$\frac{3}{5} \times - \frac{5}{3} = -1$$

l, and ly are perpendicular as mixmy=-1

