

Kinematics

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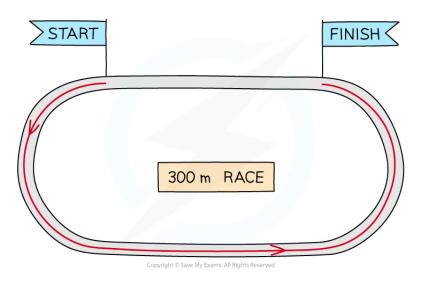
Distance & Displacement

Distance & Displacement

Distance

- **Distance** is a measure of how far an object travels
- It is a scalar quantity in other words, the direction is not important

Total running distance



The athletes run a total distance of 300 m

- Consider some athletes running a 300 m race on a 400 m track
- The **distance** travelled by the athletes is **300 m**

Displacement

- **Displacement** is a measure of how far something is from its starting position, along with its direction
 - In other words, it is the **change** in position
- It is a vector quantity it describes both magnitude and direction

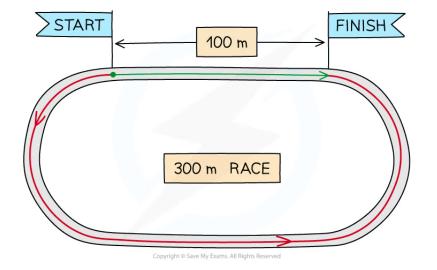
Total distance vs total displacement



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The athletes run a total distance of 300 m, but end up 100 m from where they started

Distance is a scalar quantity because...

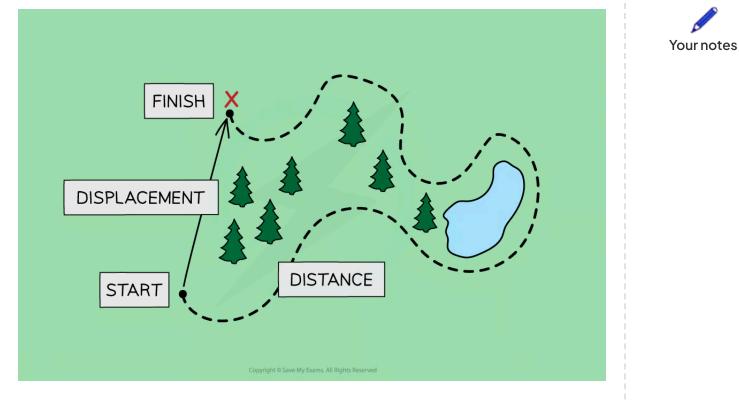
It describes how far an object has travelled overall, but not the direction it has travelled in

Displacement is a vector quantity because...

It describes how far an object is from where it started and in what direction

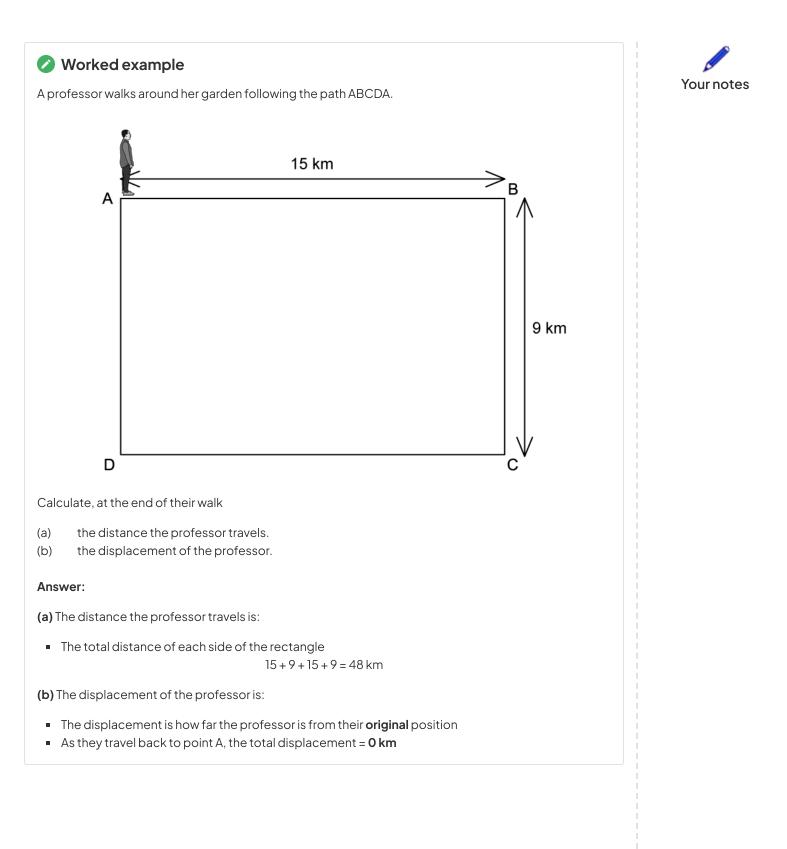
- When a student travels to school, there will probably be a **difference** in the distance they travel and their displacement
 - The **overall distance** they travel includes the total lengths of all the roads, including any twists and turns
 - The overall displacement of the student would be a straight line between their home and school, regardless of any obstacles, such as buildings, lakes or motorways, along the way

What is the difference between distance and displacement?



Displacement is a vector while distance is a scalar quantity

- Consider the same 300 m race again
 - The athletes have still run a total **distance** of **300 m** (this is indicated by the arrow in red)
 - However, their **displacement** at the end of the race is **100 m to the right** (this is indicated by the arrow in green)
 - If they ran the full 400 m, their final displacement would be **zero**



Speed & Velocity

Speed & Velocity

Speed

- The **speed** of an object is the distance it travels every second
- Speed is a **scalar** quantity
 - This is because it only contains a magnitude (without a direction)
- The **average speed** of an object is given by the equation:

$$average speed = \frac{total \, distance}{time \, taken}$$

 The SI units for speed are meters per second (m s⁻¹) but speed can often be measured in alternative units e.g. km h⁻¹ or mph, when it is more appropriate for the situation

Velocity

- The **velocity** of a moving object is similar to its speed and also describes the direction of the velocity
- Velocity is defined as:

The rate of change of displacement

• Velocity is, therefore, a vector quantity because it describes both magnitude and direction

The difference between speed and velocity

- Speed is a scalar quantity whilst velocity is vector
 - Velocity is the speed in a given direction



The cars in the diagram above have the same speed (a scalar quantity) but different velocities (a vector quantity). Fear not, they are in different lanes!

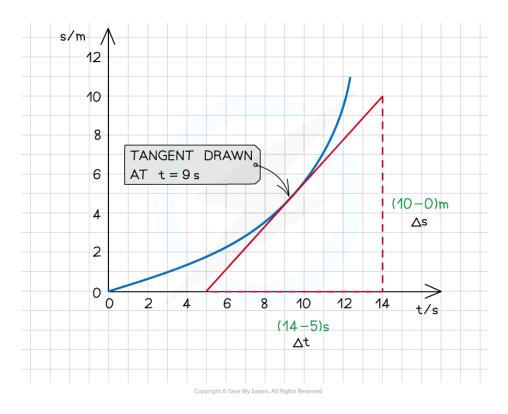
- This means velocity can also have a **negative** value
 - E.g. a ball thrown upwards at a velocity of 3 m s⁻¹ comes down at a velocity –5 m s⁻¹, if upwards is considered positive
 - However, their **speeds** are still 3 m s⁻¹ and 5 m s⁻¹ respectively

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Instantaneous Speed & Velocity

- The instantaneous speed (or velocity) is the speed (or velocity) of an object at any given point in time
- This could be for an object moving at a constant velocity or **accelerating**
 - An object at constant velocity is shown by a straight line on a displacement time graph
 - An object accelerating is shown by a curved line on a displacement time graph
 - An accelerating object will have a changing velocity
- To find the instantaneous velocity on a displacement-time graph:
 - Draw a **tangent** at the required time
 - Calculate the gradient of that tangent



The instantaneous velocity is found by drawing a tangent on the displacement time graph

In the graph above, at t = 9 s, the velocity is:

gradient =
$$\frac{10 - 0}{14 - 5}$$
 = 1.11 m s⁻¹

Average Speed & Velocity

• The average velocity \overline{V} of an object can be calculated using

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$$\overline{V} = \frac{\Delta x}{\Delta t}$$

- Where:
 - ΔX = total displacement, or change in position (m)
 - Δt = total time taken (s)
- If the initial velocity u and final velocity v are known, the average velocity can also be calculated from

$$\overline{v} = \frac{(u+v)}{2}$$

- To find the average velocity on a displacement-time graph, divide the **total displacement** (on the y-axis) by the **total time** (on the x-axis)
 - This method can be used for both a curved or a straight line on a displacement-time graph

Worked example

Florence Griffith Joyner set the women's 100 m world record in 1988, with a time of 10.49 s.

Calculate her average speed during the race.

Answer:

- Sprinters typically speed up from rest to a maximum speed
- Because Florence's speed changes over the course of the race, we can calculate her average speed using the equation:

average speed = total distance ÷ time taken

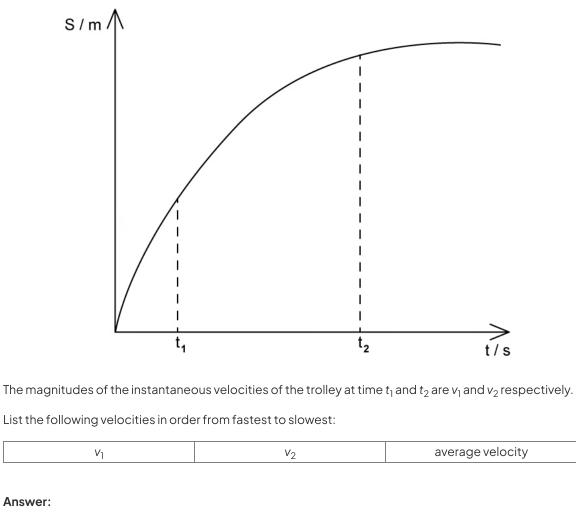
- Where:
 - Total distance, s = 100 m
 - Time taken, *t* = 10.49 s

average speed = $100 \div 10.49 = 9.5328 = 9.53 \text{ m s}^{-1}$



Worked example

The variation of displacement of a box sliding across a rough surface with time t is shown on the graph below.

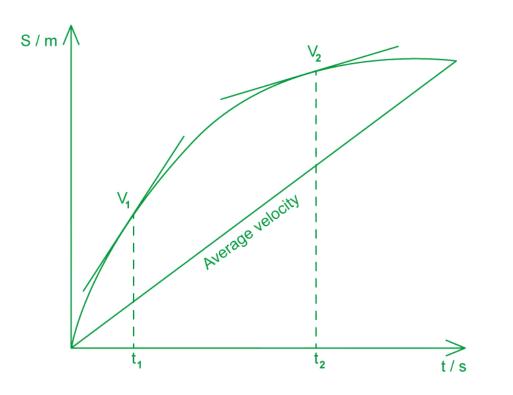


Step 1: Sketch the velocities from the graph

• The instantaneous velocity is the gradient of a tangent at a certain time

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Your notes



• The average velocity is the total displacement over the total time

Step 2: Compare the gradients of each velocity

- The fastest velocity will have the **steepest** gradient and the slowest velocity the **shallowest** gradient
- In order from fastest to slowest:

 v_1 > average velocity > v_2

Examiner Tip

When you draw a tangent to a curve, make sure it **just touches** the point at which you wish to calculate the gradient. The angle between the curve and the tangent line should be roughly equal on both sides of the point.

If you are asked to find the instantaneous velocity from a graph, you will be told the **time** at which they want this velocity for.

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Acceleration

Acceleration

Acceleration is defined as:

The rate of change of velocity

- Acceleration is a vector quantity and is measured in metres per second squared (m s⁻²)
 - It describes how much an object's velocity **changes** every **second**
- The average acceleration of an object can be calculated using:

average acceleration =
$$\frac{change in velocity}{time taken}$$

$$a = \frac{\Delta v}{\Delta t}$$

- Where:
 - $a = average acceleration (m s^{-2})$
 - ΔV = change in velocity (m s⁻¹)
 - $\Delta t = \text{total time taken (s)}$
- The **change in velocity** is the **difference** between the initial and final velocity, as written below:

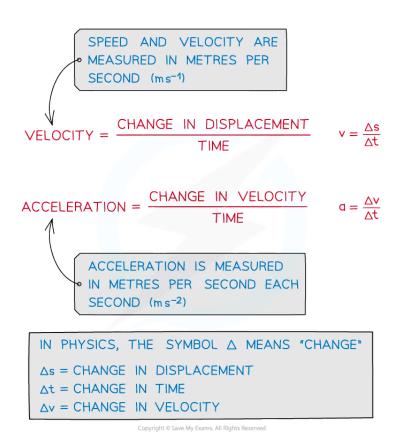
change in velocity = final velocity - initial velocity

$$\Delta v = (v - u)$$

Equations linking displacement, velocity, and acceleration



Your notes



Instantaneous Acceleration

- The instantaneous acceleration is the acceleration of an object at any given point in time
- This could be for an object with a constantly changing acceleration
 - An object accelerating is shown by a **curved line** on a velocity-time graph

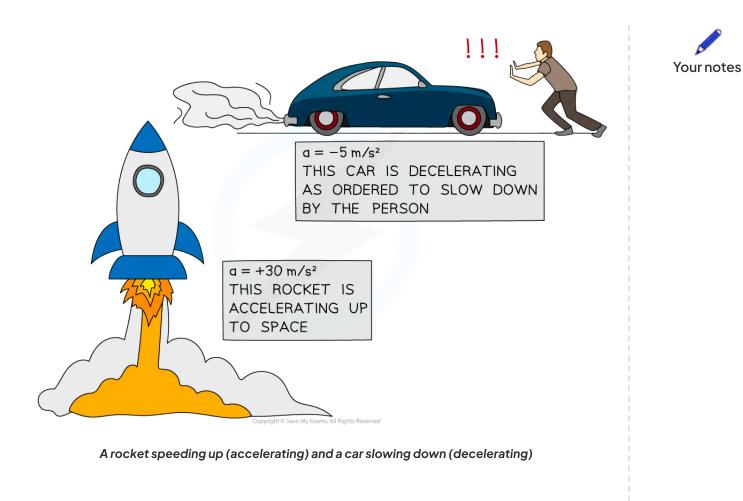
What is a negative acceleration called?

- The acceleration of an object can be positive or negative, depending on whether the object is speeding up or slowing down
 - If an object is **speeding up**, its acceleration is **positive**
 - If an object is **slowing down**, its acceleration is **negative** (deceleration)
- However, acceleration can also be negative if it is accelerating in the **negative direction**

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Worked example

A Japanese bullet train decelerates at a constant rate in a straight line.

The velocity of the train decreases from an initial velocity of 50 m s⁻¹ to a final velocity of 42 m s⁻¹ in 30 seconds.

- (a) Calculate the change in velocity of the train.
- (b) Calculate the deceleration of the train, and explain how your answer shows the train is slowing down.

Answer:

(a)

• The change in velocity is equal to

$$\Delta v = v - u$$

- Where:
 - Initial velocity, $u = 50 \text{ m s}^{-1}$
 - Final velocity, v = 42 m s⁻¹

$$\Delta V = 42 - 50 = -8 \text{ m s}^{-1}$$

(b)

• Acceleration is equal to

$$a = \frac{\Delta v}{\Delta t}$$

• Where the time taken is $\Delta t = 30$ s

$$=\frac{-8}{30}=-0.27\,\mathrm{m\,s^{-1}}$$

• The answer is **negative**, which indicates the train is **slowing down**

а

Examiner Tip

Remember the units for acceleration are **metres per second squared**, m s⁻². In other words, acceleration measures how much the velocity (in m s⁻¹) changes every second, (m s⁻¹) s⁻¹

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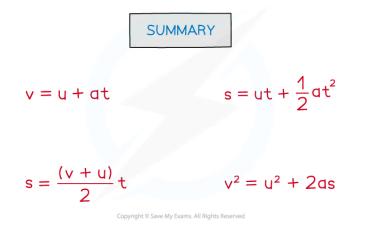
Kinematic Equations

Kinematic Equations

- The kinematic equations of motion are a set of four equations that can describe any object moving with **constant** or **uniform** acceleration
- They relate the five variables:
 - s = displacement
 - u = initial velocity
 - v = final velocity
 - a = acceleration
 - t = time interval

Kinematic Equations of Motion

• There are four kinematic equations:



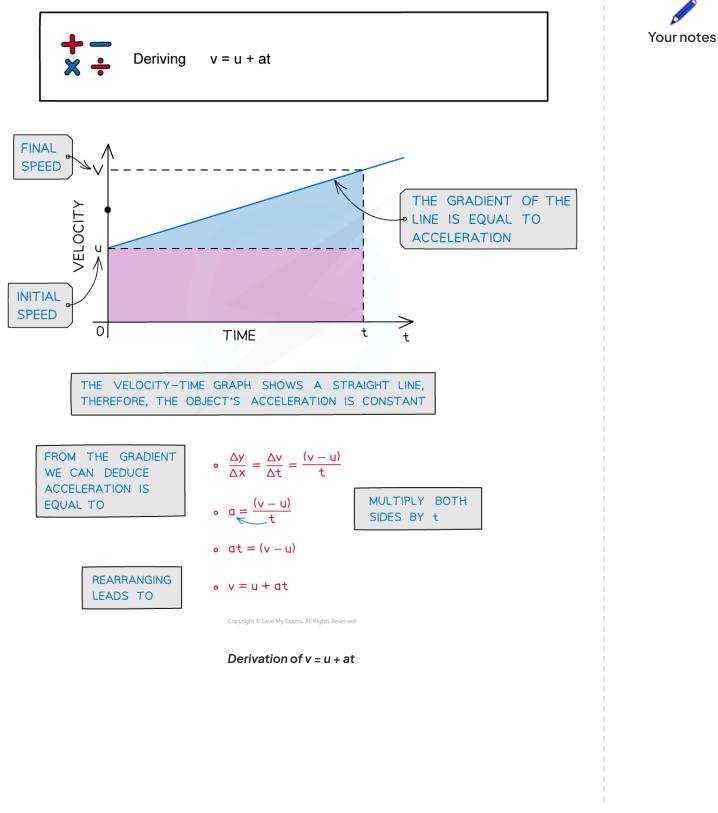
How to derive the kinematic equations



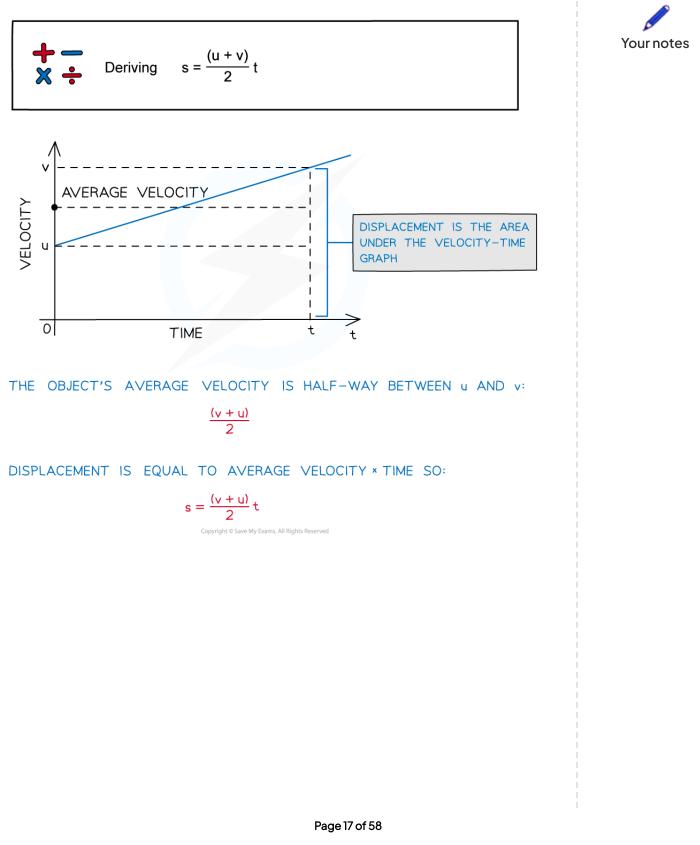
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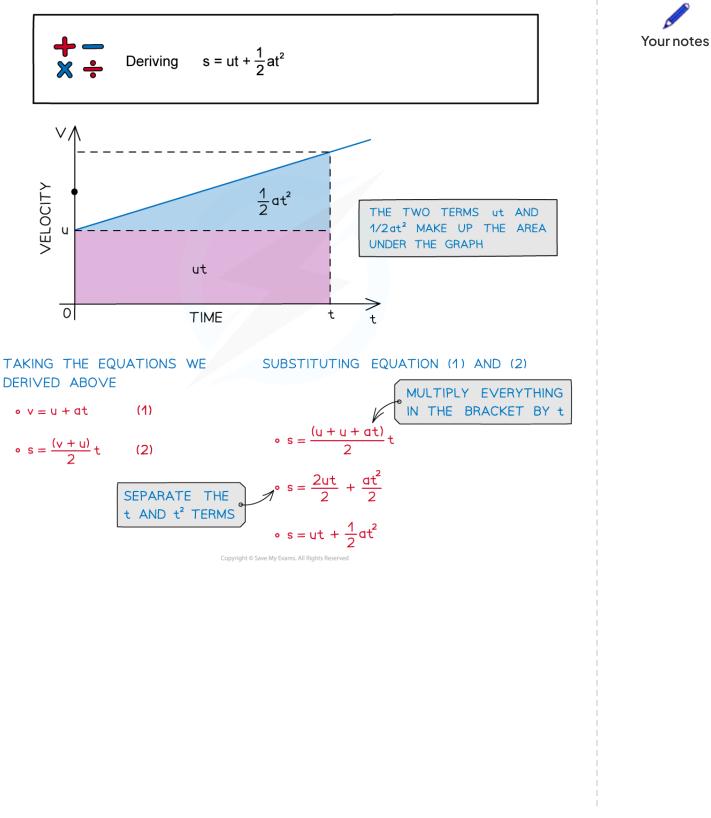


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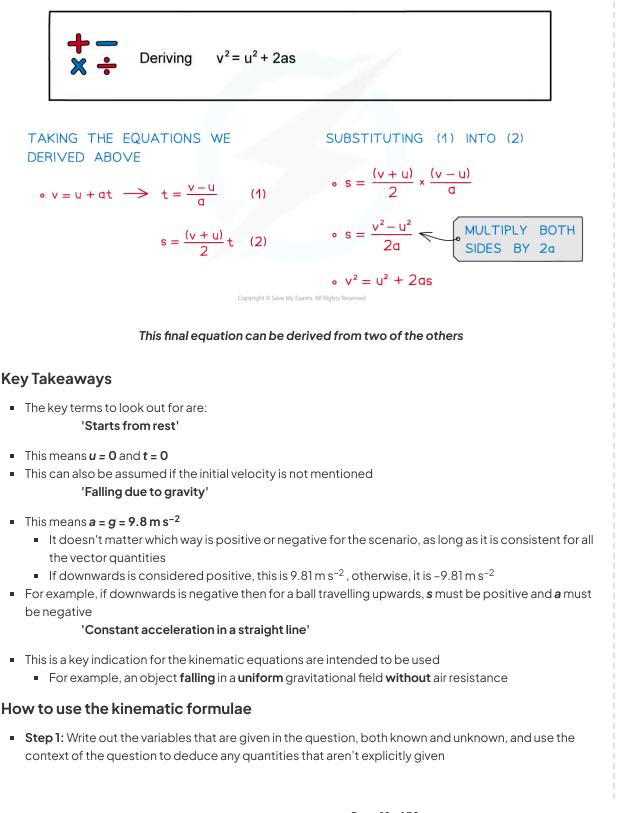


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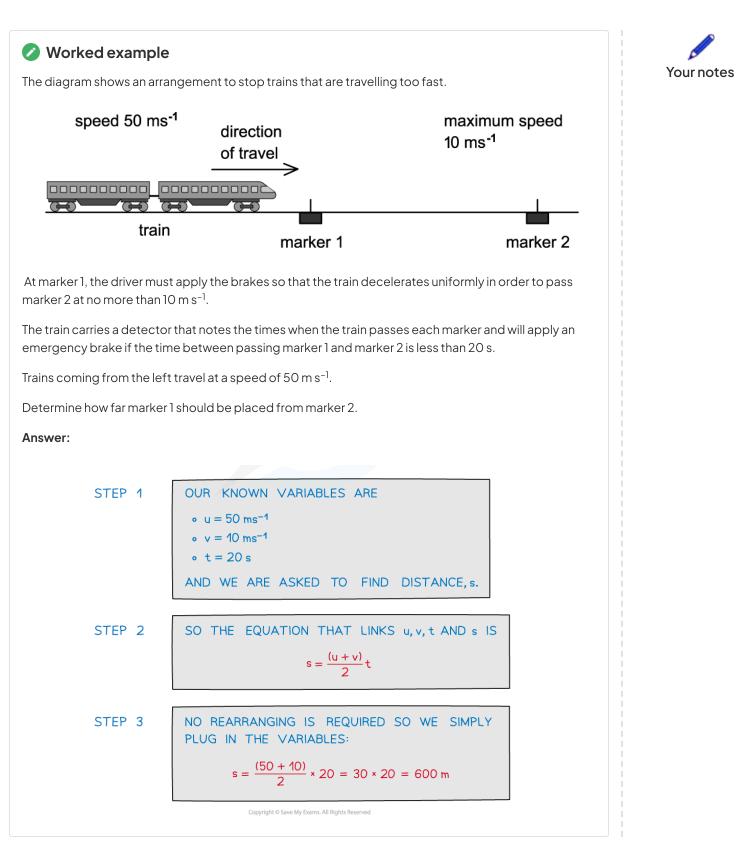


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- e.g. for vertical motion a = ± 9.81 m s⁻², an object which starts or finishes at rest will have u = 0 or v = 0
- Step 2: Choose the equation which contains the quantities you have listed
 - e.g. the equation that links s, u, a and t is $s = ut + \frac{1}{2}at^2$
- **Step 3:** Convert any units to SI units and then insert the quantities into the equation and rearrange algebraically to determine the answer





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Worked example

A cyclist is travelling directly east through a village, which is completely flat, at a velocity of 6 m s⁻¹. They then start to constantly accelerate at 2 m s^{-2} for 4 seconds.

- (a) Calculate the distance that the cyclist covers in the 4 s acceleration period.
- (b) Calculate the cyclist's final velocity after the 4 s interval of acceleration.

Later on in their journey, cyclist **A** is now cycling through a different village, at a constant velocity of 18 m s⁻¹. Cyclist **A** passes a friend, Cyclist **B** who begins accelerating from rest at a constant acceleration of 1.5 m s^{-2} in the same direction as Cyclist **A** at the moment they pass.

(c) Calculate how long it takes for Cyclist **B** to catch up to Cyclist **A**.

Answer:

(a) Calculate the displacement, s

Step 1: List the known quantities

- Initial velocity, u = 6 m s⁻¹
- Acceleration, $a = 2 \text{ m s}^{-2}$
- Time, *t* = 4 s
- Displacement = s (this needs to be calculated)

Step 2: Identify the best SUVAT equation to use

- Since the question states **constant acceleration**, the kinematic equations can be used
- In this problem, the equation that links s, u, a, and t is

$$s = ut + \frac{1}{2}at^2$$

Step 3: Substitute the known quantities into the equation

$$s = (6 \times 4) + (0.5 \times 2 \times 4^2) = 24 + 16$$

Displacement: **s = 40 m**

(b) Calculate the final velocity, v

Step 1: List the known quantities

- Initial velocity, u = 6 m s⁻¹
- Acceleration, a = 2 m s⁻²
- Time, t = 4 s
- Final velocity = v (this needs to be calculated)

Step 2: Identify and write down the equation to use

• Since the question states constant acceleration - SUVAT equation(s) - can be used

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• In this problem, the equation that links *v*, *u*, *a*, and *t* is:

$$v = u + at$$

Step 3: Substitute the known quantities into the equation

 $v = 6 + (2 \times 4)$

Final velocity: **v** = 14 m s⁻¹

(c) Calculate the time t for **B** to catch up to **A**

Step 1: List the known quantities for cyclist A

- Initial velocity, $U_A = 18 \text{ m s}^{-1}$
- Acceleration, $\boldsymbol{a}_{\boldsymbol{\Lambda}} = 0 \,\mathrm{m}\,\mathrm{s}^{-2}$
- Time = t
- Displacement = S_A

Step 2: List the known quantities for cyclist B

- Initial velocity, u = 0 m s⁻¹
- Acceleration, $a = 1.5 \text{ m s}^{-2}$
- Time = t
- Displacement = S_B

Step 3: Write expressions for Cyclist A and Cyclist B in terms of their displacement

• Cyclist **A**'s motion can be expressed by:

$$s_A = u_A t + \frac{1}{2} a_A t^2$$
$$s_A = 18t + 0 = 18t$$

• Cyclist **B**'s motion can be expressed by:

$$s_B = u_B t + \frac{1}{2} a_B t^2$$

$$s_B = 0 + \left(\frac{1}{2} \times 1.5 \times t^2\right) = \frac{3}{4}t^2$$

Step 4: Equate the two equations and solve for t

- The two equations describe the displacement of each cyclist respectively
- When equating them, this will find the time when the cyclists are at the same location

$$s_A = s_B$$

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$$18t = \frac{3}{4}t^2 \implies \frac{3}{4}t^2 - 18t = 0$$
$$(t^2 - 24t) = 0$$

• Therefore, solving for *t*, it can be two possible answers:

t = 0 s **or** t = 24 s

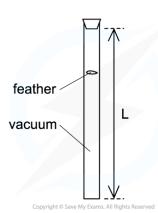
• Since the question is seeking the time when the two cyclists meet after first passing each other, the final answer is **24 s**



Worked example

A science museum designed an experiment to show the fall of a feather in a vertical glass vacuum tube.

The time of fall from rest is 0.5 s.



Use an appropriate SUVAT equation to calculate the length L of the tube.

Answer:

IN THIS PROBLEM, WE ONLY NEED TO CONSIDER VERTICAL MOTION.
FIRST WE MUST LIST THE KNOWN VARIABLES.

$$a = 9.81 \text{ ms}^{-2} \qquad u = 0 \qquad t = 0.5 \text{ s} \qquad L = ?$$
THE EQUATION THAT LINKS THESE VARIABLES IS

$$s = ut + \frac{1}{2}at^{2}$$

$$L = \frac{1}{2}gt^{2}$$

$$L = \frac{1}{2}gt^{2} = 1.2 \text{ m}$$

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Examiner Tip

This is one of the most important sections of this topic - usually, there will be one, or more, questions in the exam about solving problems with the kinematic equations equations. The best way to master this section is to practice as many questions as possible!

Watch out for the direction of vectors: displacement, acceleration and velocity. Take a single direction as positive (and hence the opposite direction is negative) and **stick with it** throughout the question, this is the most common pitfall.

Don't worry, you won't have to memorise these, they are give in your data booklet in the exam.

You may sometimes see these equations referred to as 'SUVAT' equations.



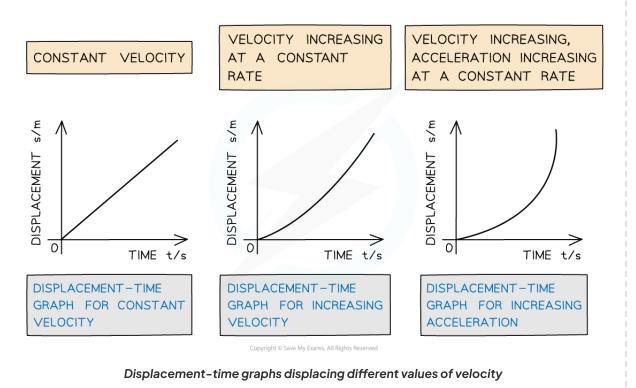
Motion Graphs

Motion Graphs

- The motion of objects can be analysed in terms of position, velocity and acceleration
 - These are all related to each other by gradients and areas under curves
- Three types of graphs that can represent the motion of an object are:
 - Displacement-time graphs
 - Velocity-time graphs
 - Acceleration-time graphs

Displacement-Time Graphs

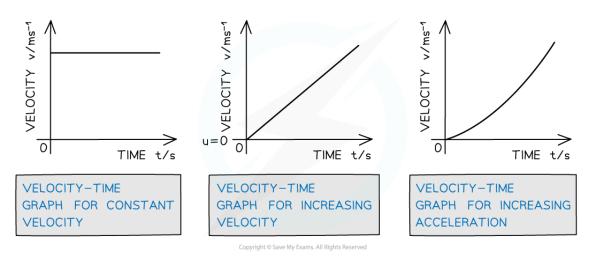
- On a **displacement-time** graph:
 - Slope equals velocity
 - The y-intercept equals the initial displacement
 - A straight (diagonal) line represents a constant velocity
 - A curved line represents an acceleration
 - A **positive slope** represents motion in the **positive direction**
 - A negative slope represents motion in the negative direction
 - A zero slope (horizontal line) represents a state of rest
 - The area under the curve is meaningless



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Velocity-Time Graphs

- On a **velocity-time** graph:
 - Slope equals acceleration
 - The y-intercept equals the initial velocity
 - A straight (diagonal) line represents uniform acceleration
 - A curved line represents non-uniform acceleration
 - A positive slope represents acceleration in the positive direction
 - A negative slope represents acceleration in the negative direction
 - A zero slope (horizontal line) represents motion with constant velocity
 - The area under the curve equals the change in displacement



Velocity-time graphs displacing different values of acceleration

Acceleration-Time Graphs

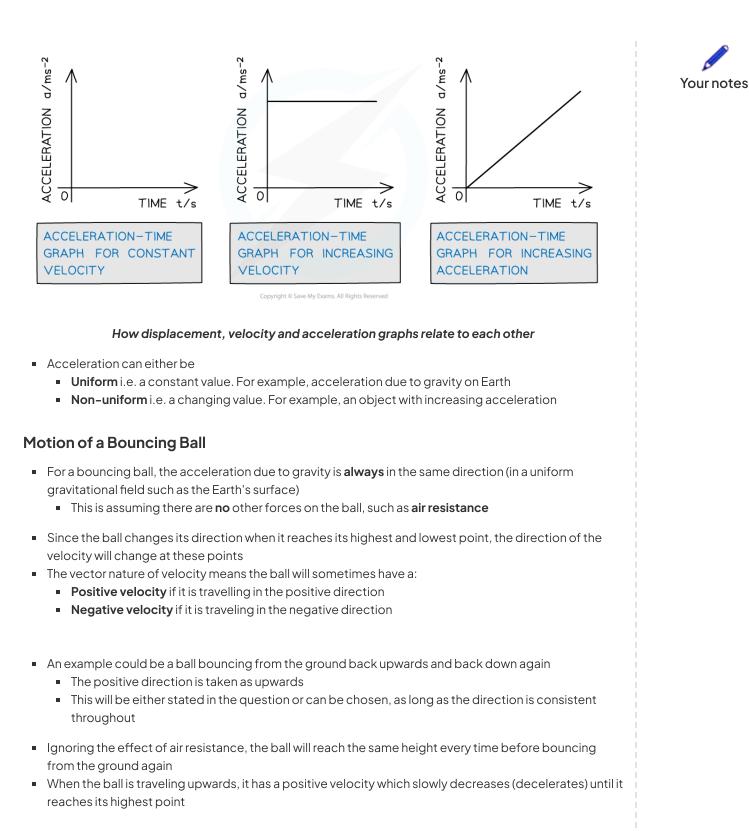
- On an acceleration-time graph:
 - Slope is meaningless
 - The y-intercept equals the initial acceleration
 - A zero slope (horizontal line) represents an object undergoing constant acceleration
 - The area under the curve equals the change in velocity



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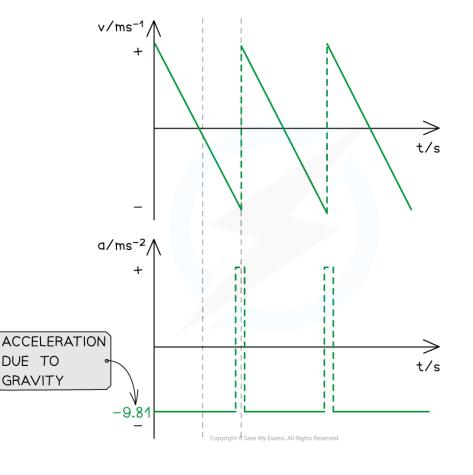


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 $\mathbf{A} \mathbf{B}$



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Your notes

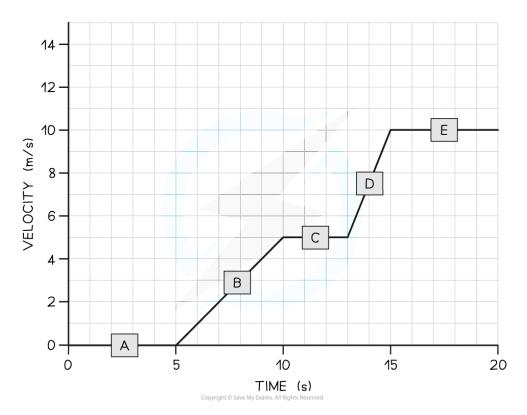
- At point **A** (the highest point):
 - The ball is at its maximum displacement
 - The ball momentarily has **zero velocity**
 - The velocity changes from positive to negative as the ball changes direction
 - The acceleration, g, is still constant and directed vertically downwards
- At point **B** (the lowest point):
 - The ball is at its **minimum displacement** (on the ground)
 - Its velocity changes instantaneously from negative to positive, but its speed (magnitude) remains the same
 - The change in direction causes a momentary acceleration (since acceleration = change in velocity / time)

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Worked example

Tora is training for a cycling tournament.

The velocity-time graph below shows her motion as she cycles along a flat, straight road.





- (a) In which section (A, B, C, D, or E) of the velocity-time graph is Tora's acceleration the largest?
- (b) Calculate Tora's acceleration between 5 and 10 seconds.

Answer:

(a)

Step 1: Recall that the slope of a velocity-time graph represents the magnitude of acceleration

- The slope of a velocity-time graph indicates the magnitude of acceleration
 Therefore, the only sections of the graph where Tora is accelerating is section B and section D
- Sections A, C, and E are flat in other words, Tora is moving at a constant velocity (i.e. not accelerating)

Step 2: Identify the section with the steepest slope

- Section D of the graph has the steepest slope
- Hence, the largest acceleration is shown in section D

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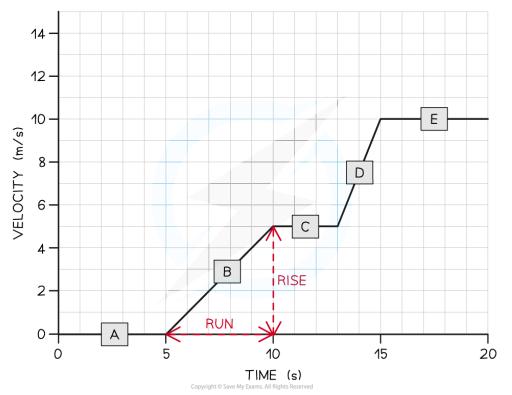
(b)

Step 1: Recall that the gradient of a velocity-time graph gives the acceleration

 Calculating the gradient of a slope on a velocity-time graph gives the acceleration for that time period

Step 2: Draw a large gradient triangle at the appropriate section of the graph

• A gradient triangle is drawn for the time period between 5 and 10 seconds below:



Step 3: Calculate the size of the gradient and state this as the acceleration

• The acceleration is given by the gradient, which can be calculated using:

acceleration = gradient =
$$\frac{5}{5}$$
 = 1 m s⁻²

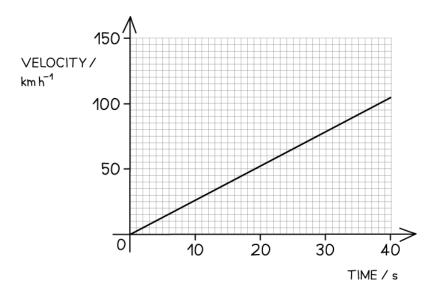
- Therefore, Tora accelerated at 1 m s $^{-2}$ between 5 and 10 seconds



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Worked example

The velocity-time graph of a vehicle travelling with uniform acceleration is shown in the diagram below.



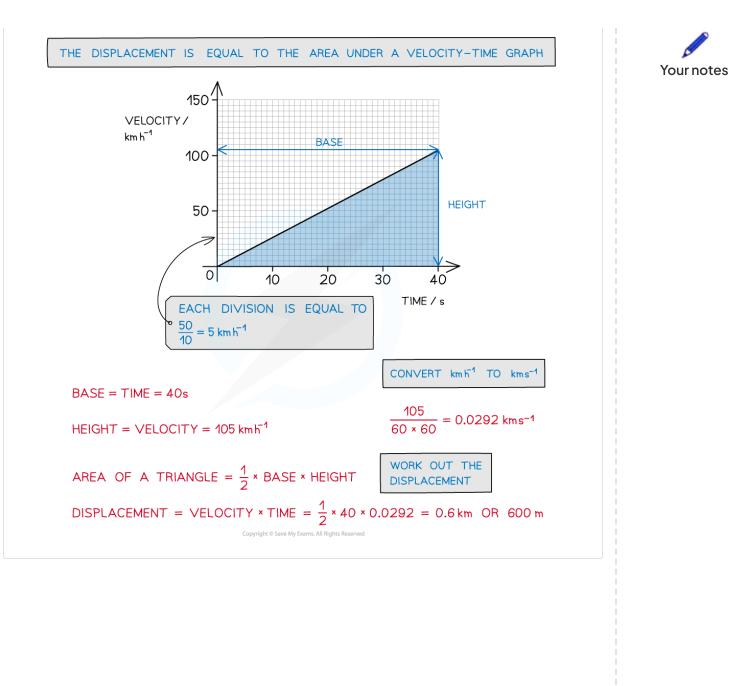
Calculate the displacement of the vehicle at 40 s.

Answer:

Your notes

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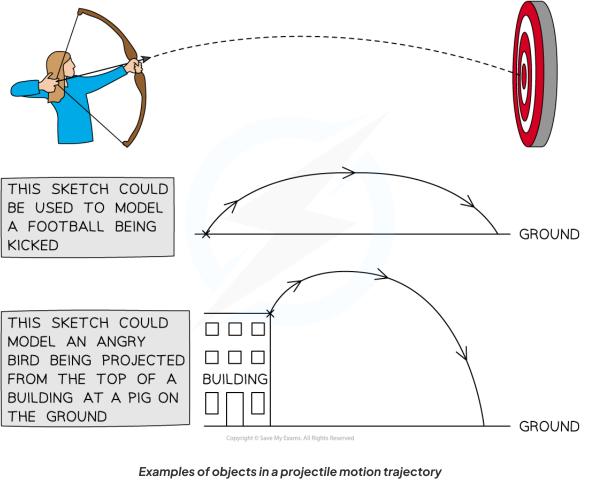


Projectile Motion

Projectile Motion

What is a projectile?

- A **projectile** is a particle moving freely (non-powered), under gravity, in a two-dimensional plane
- Examples of projectile motion include throwing a ball, jumping off a diving board and hitting a baseball with a baseball bat
- In these examples, it is assumed that:
 - Resistance from the air or liquid (known as fluid resistance) the object is travelling through is negligible
 - Acceleration due to free-fall, g is constant as the object is moving close to the surface of the Earth



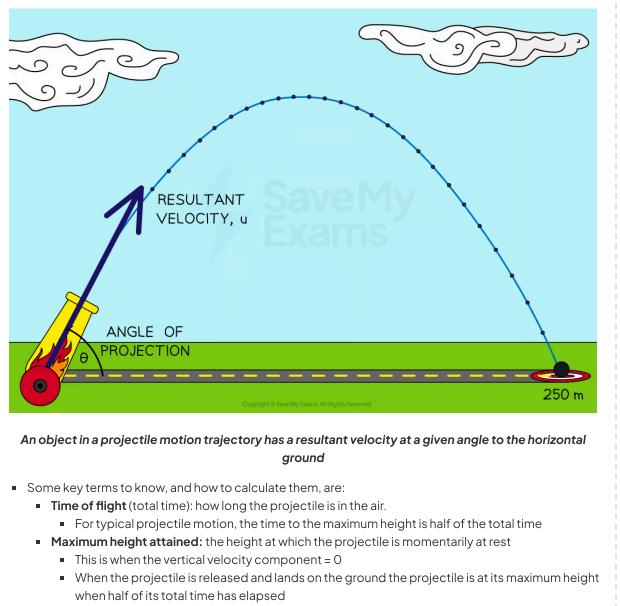
- An object is sent into a projectile motion trajectory with a resultant velocity, u at an angle, θ to the horizontal
 - Examples of this include a ball thrown from a height and a cannonball launched from a cannon

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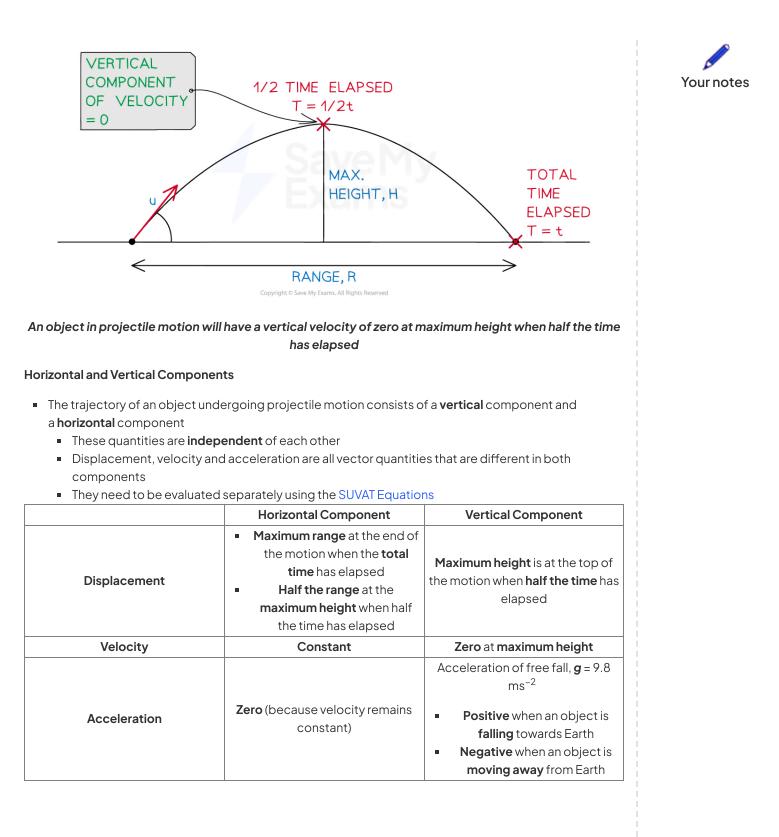


• **Range:** the horizontal distance travelled by the projectile

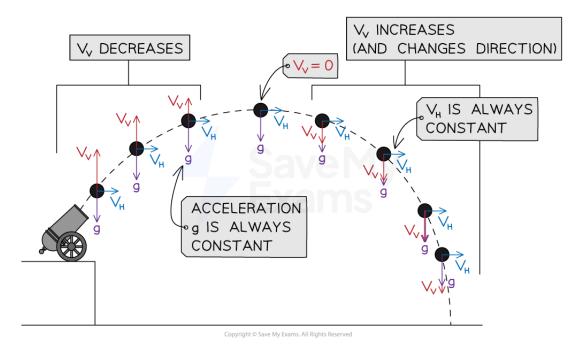
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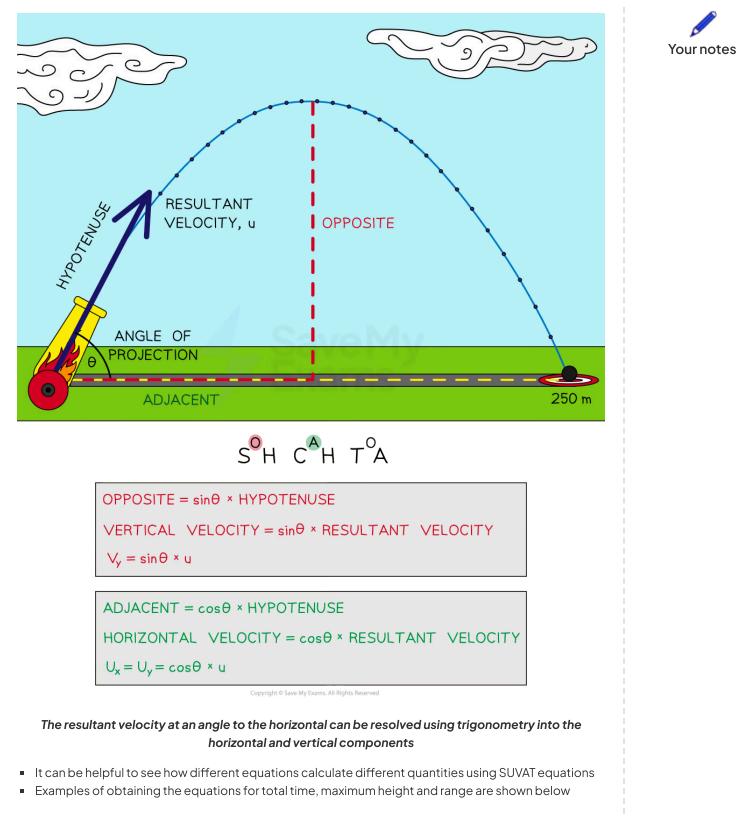
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Acceleration and horizontal velocity are always constant whilst vertical velocity changes

- The **resultant velocity** of an object in projectile motion can be split into its **horizontal** and **vertical** vector components using trigonometry where:
 - Vertical component = opposite side of the projectile triangle
 - opposite = $\sin\theta \times hyp = u \sin\theta$
 - Horizontal component = adjacent side of the projectile triangle
 - adjacent = $\cos\theta \times hyp = u\cos\theta$

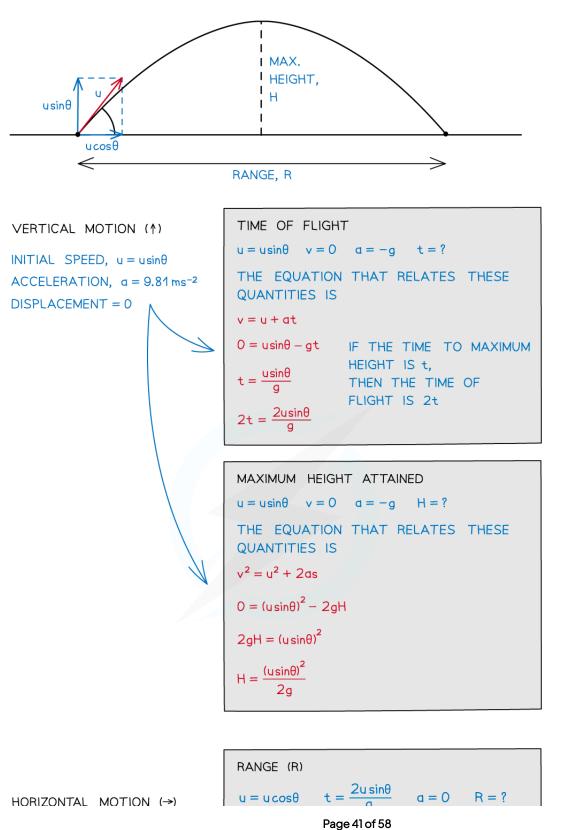
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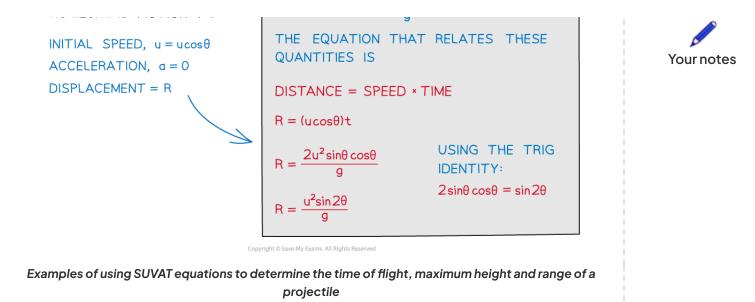
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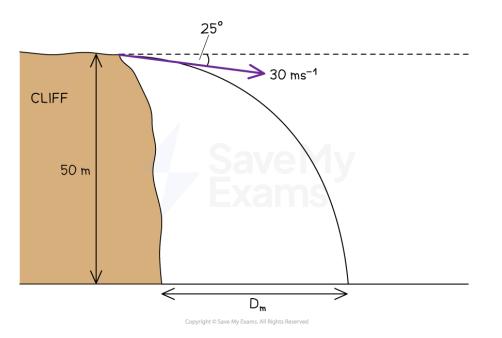


Solving problems with projectiles

- You may be required to calculate the missing quantities from the following projectile motion scenarios:
 - Vertical projection above the horizontal
 - Vertical projection below the horizontal
 - Horizontal projection
 - **Projection** at an **angle**, the most common scenario

Worked example

A stone is dropped from the top of a cliff 50.0 m high at an angle of 25.0° below the horizontal. The stone has an initial speed of 30.0 ms^{-1} and follows a curved trajectory. The stone hits the ground at a horizontal distance *D* from the base of the cliff with a vertical velocity of 33.8 ms^{-1} .



Calculate the distance D.

Answer:

Step 1: Understand the information given in the question

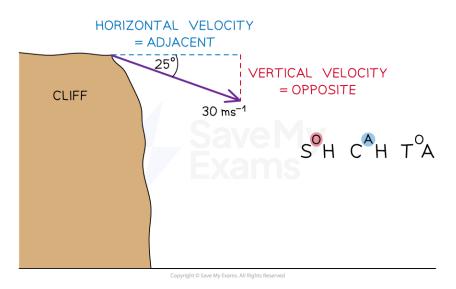
- The final vertical velocity of the stone, $v = 33.8 \text{ ms}^{-1}$
- The horizontal velocity will remain constant throughout the motion
- The question wants us to calculate the range of the stone
- The vertical acceleration is +g ms⁻²

Step 2: Resolve velocity into the vertical and horizontal components

 ${\sf Draw}\ {\rm a}\ {\rm triangle}\ {\rm on}\ {\rm the}\ {\rm diagram}\ {\rm to}\ {\rm show}\ {\rm the}\ {\rm vertical}\ {\rm and}\ {\rm horizontal}\ {\rm velocity}\ {\rm components}$



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Calculate the initial vertical component of velocity, u_v using trigonometry:

- $u_v = opposite side$
- $u_v = \sin\theta \times \text{hypotenuse side}$
- $u_v = \sin(25) \times 30 = 12.68 \text{ ms}^{-1}$

Calculate the initial horizontal component of velocity, *u_H* using trigonometry:

- $u_H = adjacent side$
- $u_H = \cos\theta \times \text{hypotenuse side}$
- $u_H = \cos(25) \times 30 = 27.19 \text{ ms}^{-1}$

Step 3: Consider the equations of motion in the vertical and horizontal directions

	Vertical Motion	Horizontal Motion
u	12.68 ms ⁻¹	27.19 ms ⁻¹
v	33.8 ms ⁻¹	27.19 ms ⁻¹
а	+9.81 ms ⁻²	0 ms ⁻²
t		
S	50 m	Dm?

Step 4: Calculate the time of flight from the vertical motion

Your notes

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$$t = \frac{33.8 - 12.68}{9.81}$$
$$t = 2.15 \,\mathrm{s}$$

Step 5: Calculate the range of the stone, D using the elapsed time and horizontal motion

s = ut D = 27.19 × 2.15

D = 58.46 m = 58 m (2 s.f.)

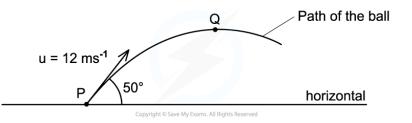


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Worked example

A ball is thrown from a point P with an initial velocity u of 12 m s^{-1} at 50° to the horizontal.

What is the value of the maximum height at Q? (ignoring air resistance)



Answer:

Step 1: Consider the situation

In this question, vertical motion only needs to be considered to find the vertical height
 Step 2: List the known quantities

- $u = 12\sin(50) \,\mathrm{ms}^{-1}$
- $v = 0 \, \text{ms}^{-1}$
- $a = -9.81 \,\mathrm{ms}^{-2}$
- s=?

Step 3: State the correct kinematic equation

$$v^2 = u^2 + 2as$$

Step 4: Rearrange the equation to make height, s the subject

$$\frac{v^2 - u^2}{2a} = s$$

Step 5: Substitute in the known quantities and calculate maximum height, s

$$s = \frac{0^2 - (12\sin(50))^2}{2 \times -9.81}$$
$$s = -4.3 \text{ m}$$

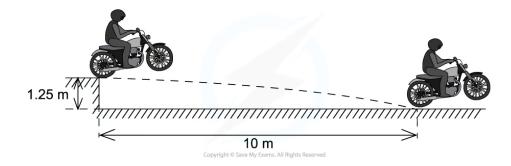
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Your	notes

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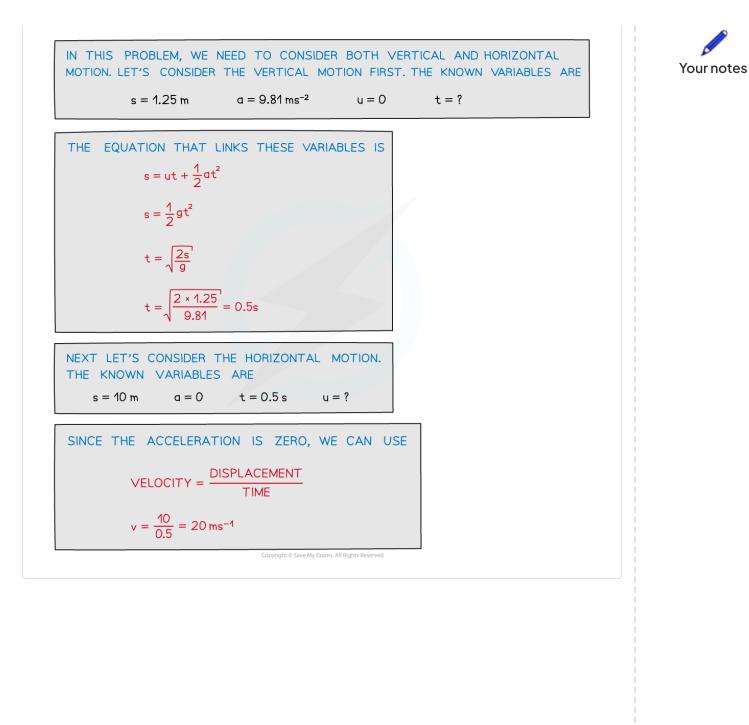
Worked example

A motorcycle stunt-rider moving horizontally takes off from a point 1.25 m above the ground, landing 10 m away as shown.

What was the speed at take-off? (ignoring air resistance)



Your notes



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Examiner Tip

Make sure you don't make these common mistakes:

- Mixing up positive and negative values for vectors
- Mixing up velocities and distances between horizontal and vertical motion
- Confusing the direction of $\sin \theta$ and $\cos \theta$
- Not converting units (mm, cm, km etc.) to metres

Further, it is worth noting that projectile motion is typically **symmetrical** when air resistance is **ignored** allowing for use of the peak to find the time of total flight or total horizontal distance by doubling the amount to get from the start point to the peak.

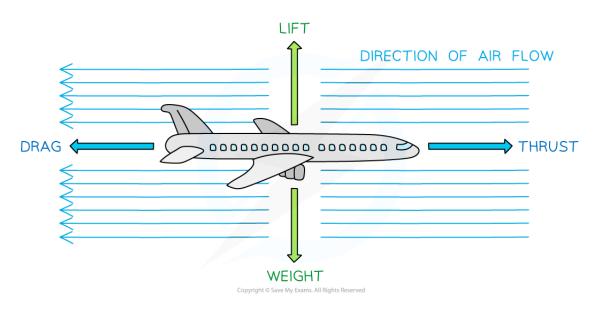
In these exam questions, unless specified, fluid resistance can be **ignored**



Fluid Resistance

Fluid Resistance

- Fluid resistance refers to the effects of gases and liquids on the motion of a body
- When an object moves through a fluid (a gas or a liquid), there are **resistive** forces for that movement
 - These forces are known as **viscous drag**
 - Viscous drag, also known as air resistance, is a type of friction
- Frictional forces:
 - Always act in the **opposite** direction to the motion of the object
 - Never speed an object up or start them moving
 - Always slow down an object or keep them moving at a constant speed
 - Always transfer energy away from the object to the surroundings
- Lift is an upward force on an object moving through a fluid. It is perpendicular to the fluid flow
 - For example, as an aeroplane moves through the air, the aeroplane pushes down on the air to change its direction
 - This causes an equal and opposite reaction as the air pushes upwards on the wings of the aeroplane (lift) due to Newton's Third Law

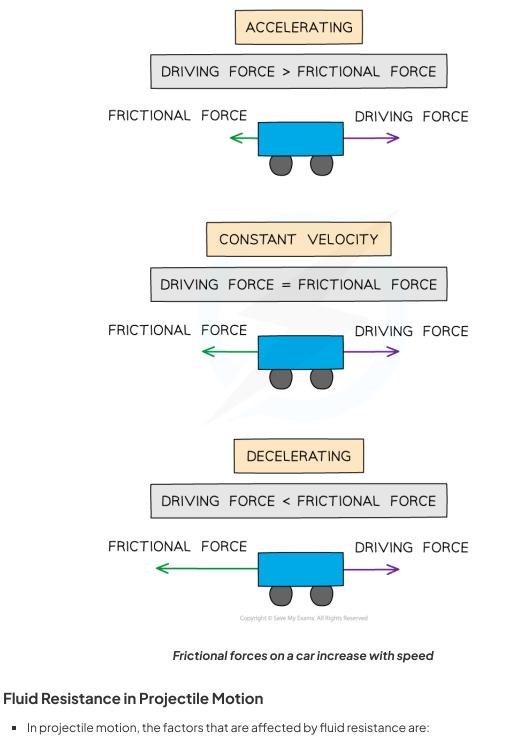


Drag forces are always in the opposite direction to the thrust (direction of motion). Lift is always in the opposite direction to the weight

- A key component of drag forces is that they increase with the **speed** of the object
- This is shown in the diagram below:

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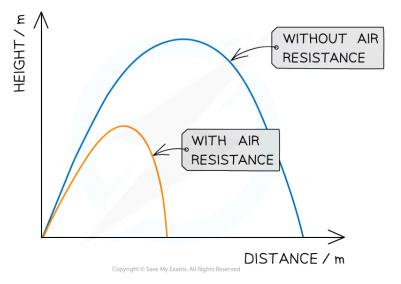
- Time of flight
- Horizontal velocity
- Horizontal acceleration

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Your notes

- Range
- Shape of trajectory
- Air resistance is the frictional force which has the most significant effect on a projectile
- Air resistance decreases the **horizontal** component of the velocity of a projectile
 - This means both its **range** and **maximum height** will decrease compared to an identical situation with no air resistance (like a vacuum)



A projectile with air resistance travels a smaller distance and has a lower maximum height than one without air resistance

- When air resistance is applied, the path of the projectile no longer follows a parabola shape
 - Its path is now **steeper** on the way down than it is up
- The flight time will also **decrease** as the projectile is in the air for a **shorter** period of time
 - This is due to having a smaller range and lower maximum height
- In summary:

Air resistance affects	Effect of air resistance
time of flight	decreases
horizontal velocity	decreases
horizontal deceleration	increases
range	decreases
shape of trajectory	no longer a parabola

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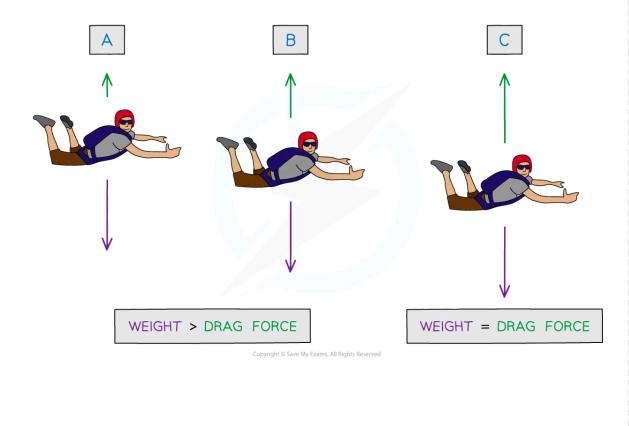
- The angle and launch speed of a projectile can be varied to cover a longer range or reach a greater maximum height, depending on the situation
 - For sports, such as the long jump or javelin, an optimum angle against air resistance is used to produce the greatest range (distance)
 - For gymnastics or ski jumper, the initial vertical velocity is made as large as possible to reach a greater maximum height and longer flight path



Terminal Speed

Terminal Speed

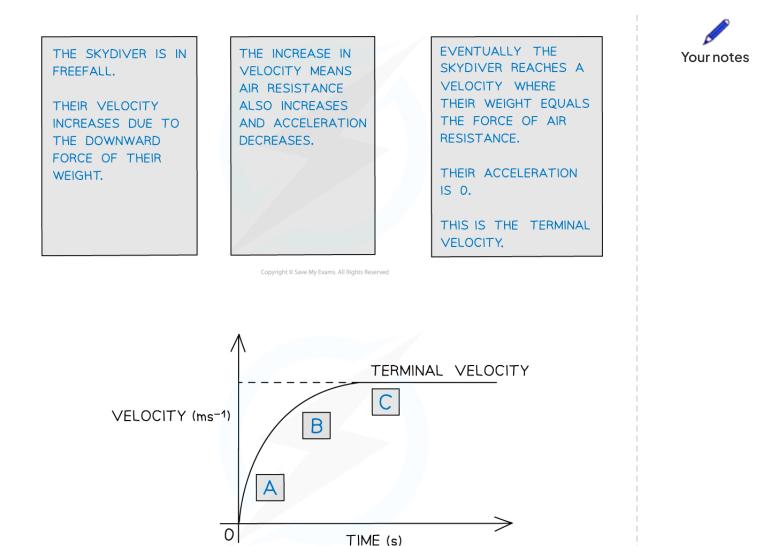
- For a body in free fall in a vacuum, the only force acting is weight, and its acceleration g is only due to gravity
- The frictional force from fluid resistance increases as the body accelerates
 This increase in velocity means the viscous drag force also increases
- Due to Newton's Second Law, this means the resultant force and therefore acceleration decreases (recall F = ma)
- When the viscous drag force is equal to the weight on the body, the body will no longer accelerate and will fall at a constant velocity
- This velocity is called the terminal velocity
- Terminal velocity can occur for objects falling through a gas or a liquid





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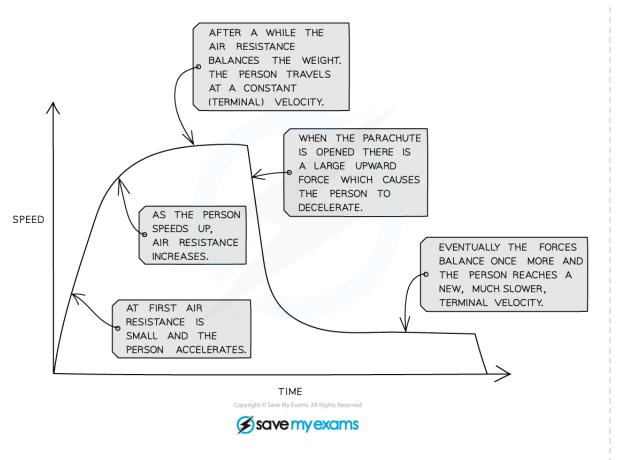
A skydiver in freefall reaching terminal velocity

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- The graph shows how the velocity of the skydiver varies with time
- Since acceleration is equal to the **gradient** of a velocity-time graph, it can be seen that
 - The acceleration **decreases**
 - The acceleration eventually becomes zero when terminal velocity is reached
- After the skydiver deploys their parachute, they decelerate to a **lower terminal velocity** to reduce the impact on landing
- This is demonstrated by the graph below:

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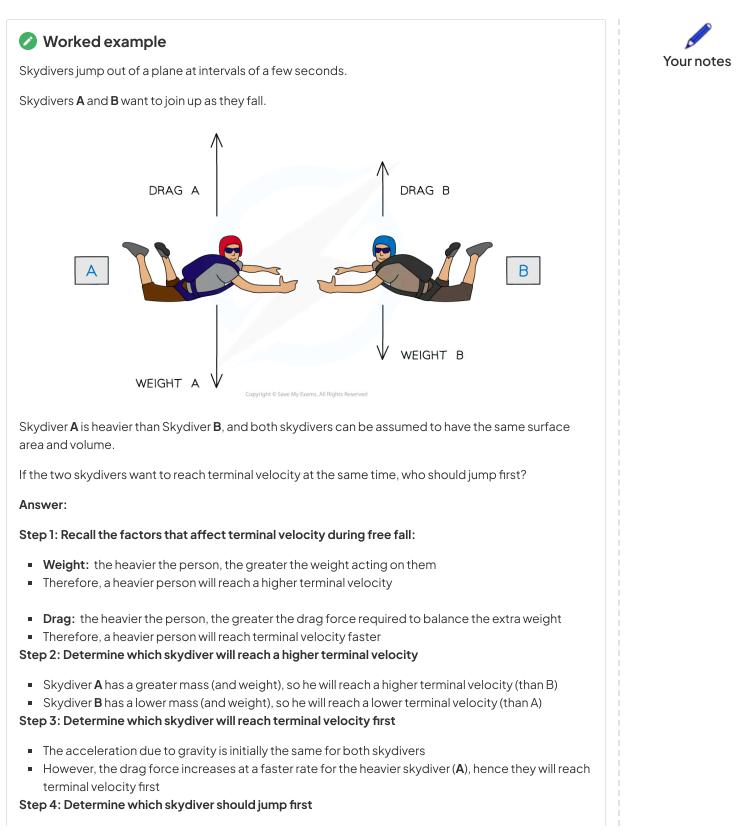
Your notes



A graph showing the changes in speed of the skydiver throughout their entire journey in freefall

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- Skydiver **B** should jump first since he will take longer to reach terminal velocity
- This is because skydiver **A** has a higher mass, and hence, weight
- More weight means a greater speed, therefore, **A** will reach terminal velocity faster than **B**

Examiner Tip

A common misconception is that skydivers move upwards when their parachutes are deployed - however, this is not the case, they are in fact **decelerating** to a lower terminal velocity.

If a question considers air resistance to be **'negligible**' this means in that question, air resistance is taken to be so small it will not make a difference to the motion of the body. You can take this to mean there are no drag forces acting on the body.

